

# Tone, computation, and phonological theory

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- The computational perspective on phonology teaches us much about the nature of tone
- Phonological tone teaches us much about the computational nature of phonology

Hyman (2011):

“[T]one can do everything that segmental and metrical phonology can do, but the reverse is not true. This is especially true of the long-distance effects that tone exhibits both within and across words. ...

**[A]nyone who is interested in the outer limits of what is possible in phonology would thus be well-served to understand how tone systems work.”**

- **Theoretical computational phonology:**

What computational principles define the outer limits of what is possible in phonology?

Heinz (2018):

There are computational laws that make “strong predictions ... about which logically possible phonological generalizations are not humanly possible ones.”

## This talk is about...

- how, **computationally, tone is different** than segmental<sup>1</sup> phonology
- what the **limits** are of cross-linguistic variation in tone
- how the computational study of tone leads to novel insights about **representations** and **learning** in phonology *as a whole*

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<sup>1</sup>..and metrical?

# Computation and typology

- What are possible...
  - well-formedness constraints (**phonotactics**)?  
(Chomsky and Halle, 1965; Kisseberth, 1970; Prince and Smolensky, 1993)
  - maps from underlying representations to surface representations (**processes**)?  
(Chomsky and Halle, 1968; Prince and Smolensky, 1993)

## Computation and typology

- **Attested:** all sibilants agree in [ $\pm$ anterior]:

[f-api-tʃ <sup>h</sup> ol-it]	‘I have a stroke of good luck’
[s-api-ts <sup>h</sup> ol-us]	‘he has a stroke of good luck’
[f-api-tʃ <sup>h</sup> ol-uf-waf]	‘he had a stroke of good luck’
[ha-f-xintila-waf]	‘his former Indian name’
*[s-api-tʃ <sup>h</sup> ol-us]	
*[ha-s-xintila-waf]	

Inseño Chumash (Applegate, 1972)

## Computation and typology

- **Unattested**: even and odd sibilants agree in [ $\pm$ anterior]:

[ha-ʃ-xintila-waʃ]  
[ʃ-api-tʃ<sup>h</sup>ol-us-was]  
\*[ha-s-xintila-waʃ]  
\*[s-api-tʃ<sup>h</sup>ol-us-waʃ]

“Agreeing pairs” (not attested)

- Predicted by ABC in OT

(McMullin and Hansson, 2019)



## Computation and typology

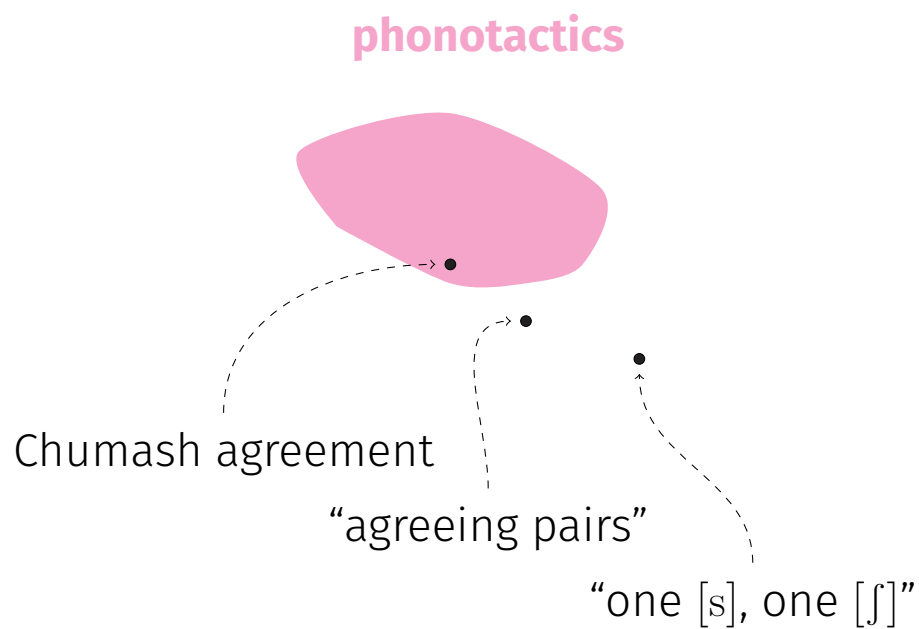
- **Unattested**: for each [−ant] sibilant there is exactly one following [+ant] sibilant:

[ha-s-xintila-waf]	*[ha-ʃ-xintila-waf]
[s-api-ts <sup>h</sup> ol-uf-waf]	*[ʃ-api-tʃ <sup>h</sup> ol-uf-waf]
[sasasafafafa]	*[sasafafafafa]

“One [s], one [ʃ]” (not attested)

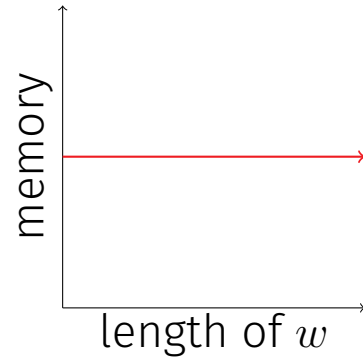
- Analogue of center embedding in syntax (Chomsky, 1956)

# Computation and typology

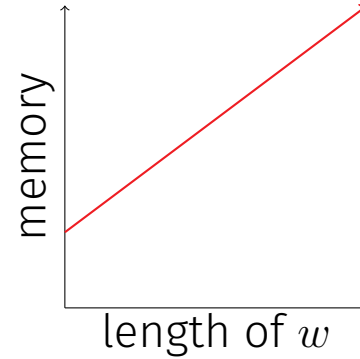


# Computation and typology

- Johnson (1972); Kaplan and Kay (1994): phonology is **regular**

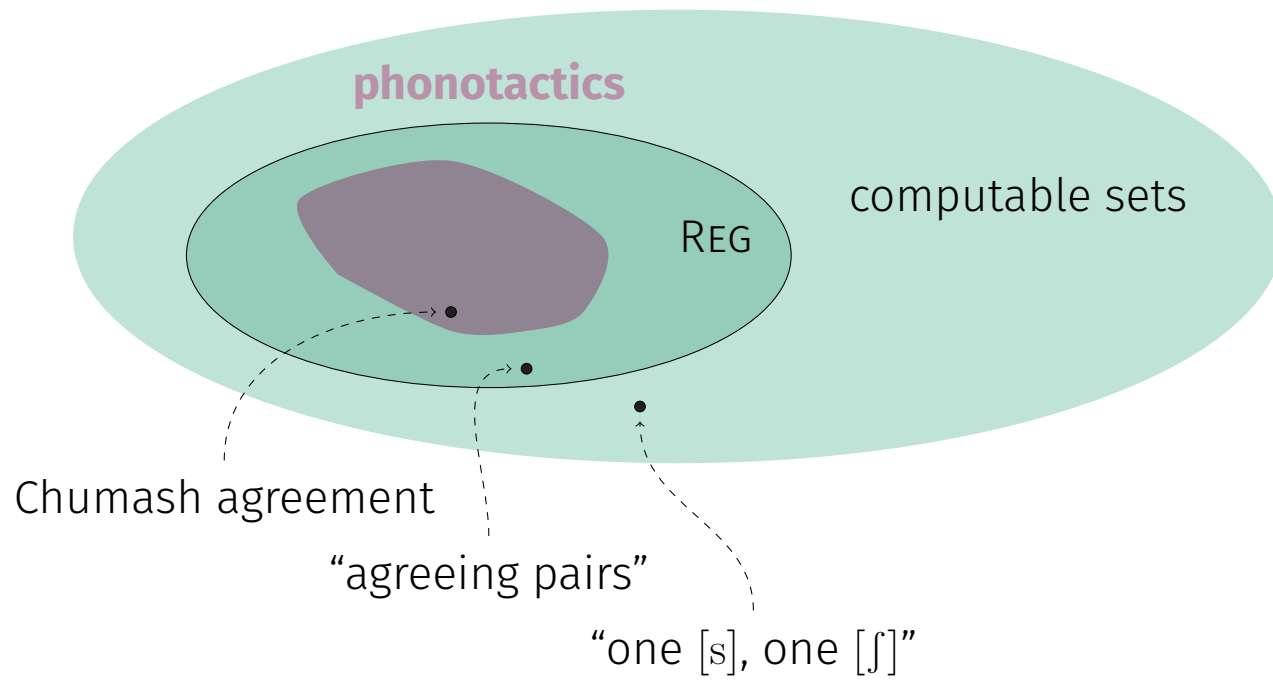


**regular**

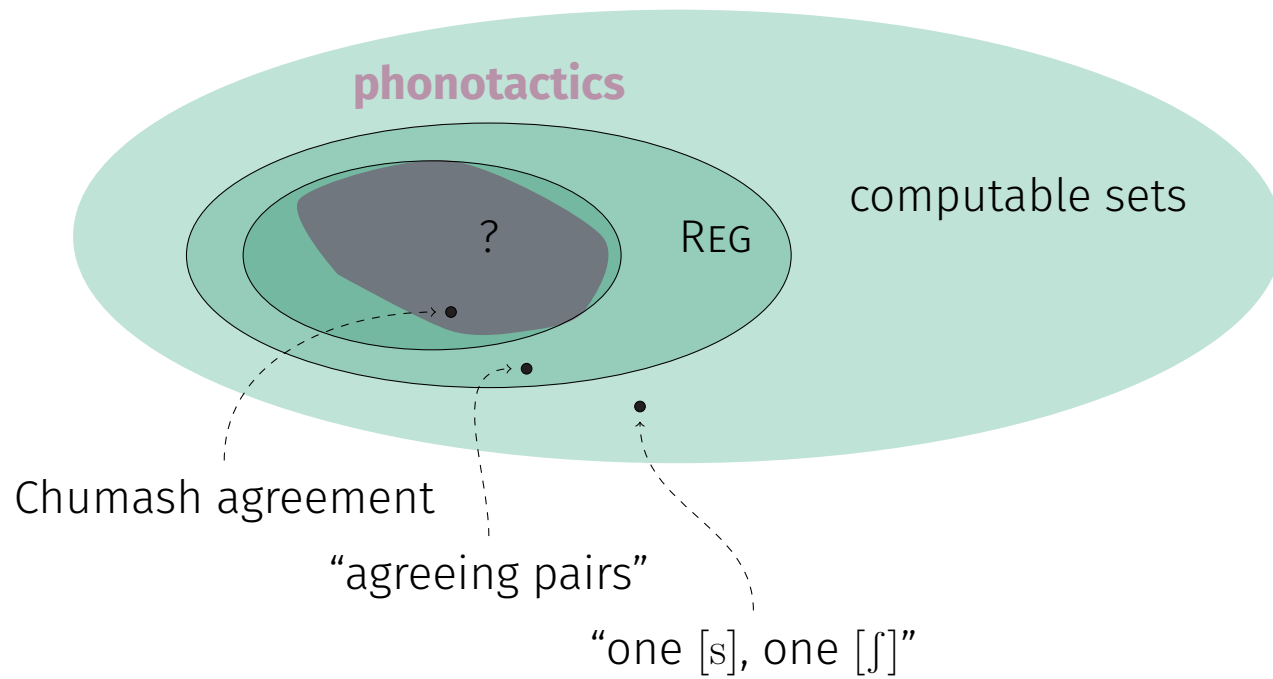


**non-regular**

# Computation and typology



# Computation and typology

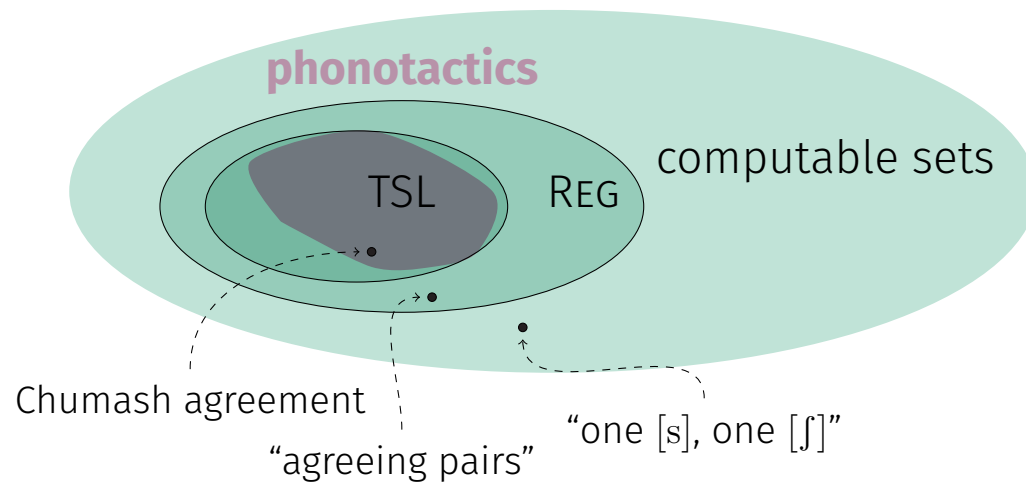


# Computation and typology

- What are possible...
  - well-formedness constraints (**phonotactics**)?  
(Chomsky and Halle, 1965; Kisseberth, 1970; Prince and Smolensky, 1993)
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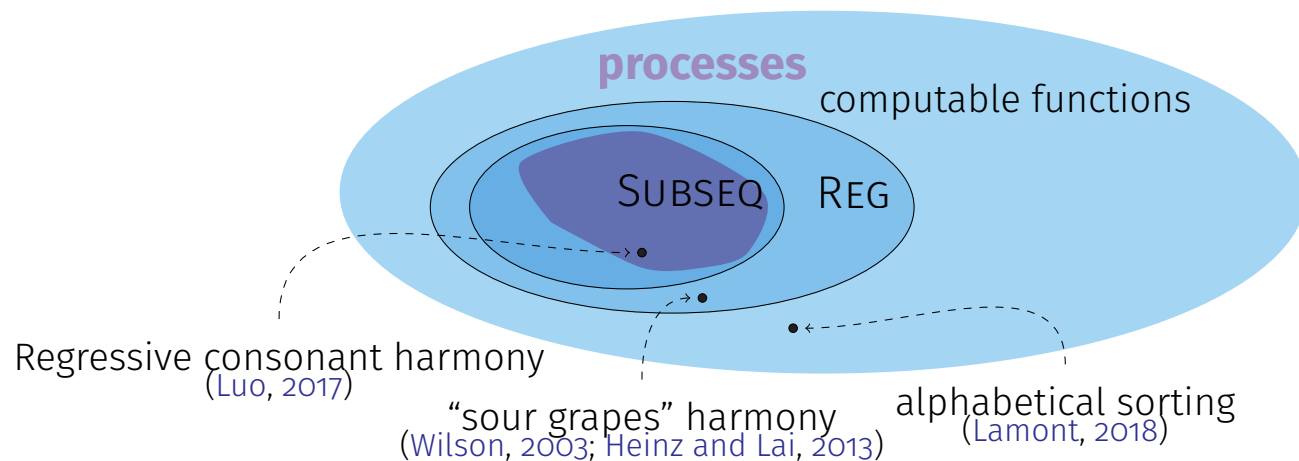
# Computation and typology

- Phonotactics are **sub-regular sets** (Heinz, 2009, 2010)
  - Hypothesis: phonotactics are **tier-based strictly local**  
(Heinz et al., 2011; McMullin and Hansson, 2019)



# Computation and typology

- Processes are sub-regular **functions** (Heinz and Lai, 2013, et seq.)
  - Hypothesis: processes are **subsequential** (Heinz and Lai, 2013; Payne, 2017; Luo, 2017)



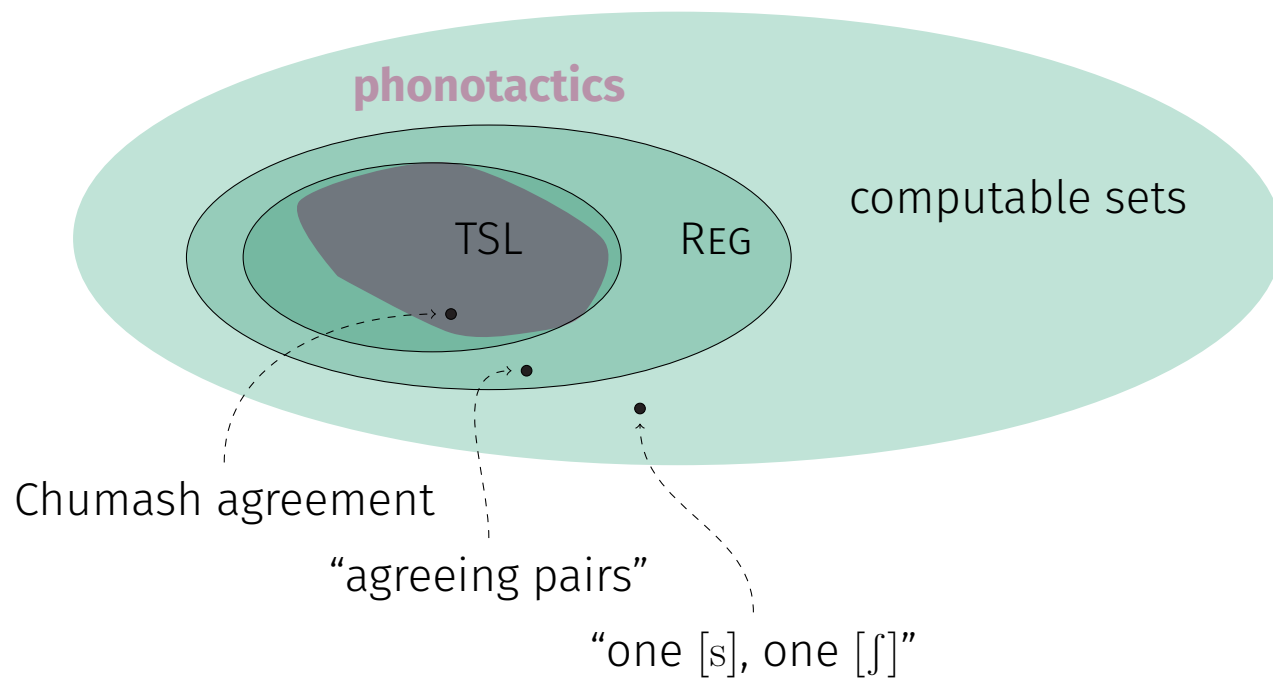


## Computation and tone

- Both hypotheses fail with tone:
  - Tonal phonotactics are *not* tier-based strictly local  
(Graf, 2017; Jardine, 2019, to appear)
  - Tonal processes are *not* subsequential (Jardine, 2016)
- However, many tonal...
  - phonotactics are **melody-local** (Jardine, to appear)
  - processes are **input melody-local**  
(Mamadou and Jardine, in progress)

# **Tonal phonotactics and melody-local grammars**

# Tier-based strictly local sets





## Tier-based strictly local sets

- Long-distance phonotactics are not local in this way (Heinz, 2010)

Chumash \*s...ʃ

# h a ʃ x i n t i l a w a ʃ #      'his former Indian name'

# h a s x i n t i l a w a ʃ #      (ill-formed)

## Tier-based strictly local sets

- A strategy is to adopt a **tier-projection**

(Hayes and Wilson, 2008; Heinz et al., 2011; McMullin and Hansson, 2019)

Chumash sibilant tier

# h a ∫ x i n t i l a w a ∫ #      'his former Indian name'

# h a s x i n t i l a w a ∫ #      (ill-formed)

# Tier-based strictly local sets

- A strategy is to adopt a **tier-projection**

(Hayes and Wilson, 2008; Heinz et al., 2011; McMullin and Hansson, 2019)

Chumash \* $\int$  with sibilant tier

$\int$   $\int$   
# h a  $\int$  x i n t i l a w a  $\int$  # 'his former Indian name'

s  $\int$  X  
# h a s x i n t i l a w a  $\int$  # (ill-formed)

# Tier-based strictly local sets

- **Tier-based strictly local:** local on a tier-projection

(Heinz et al., 2011)

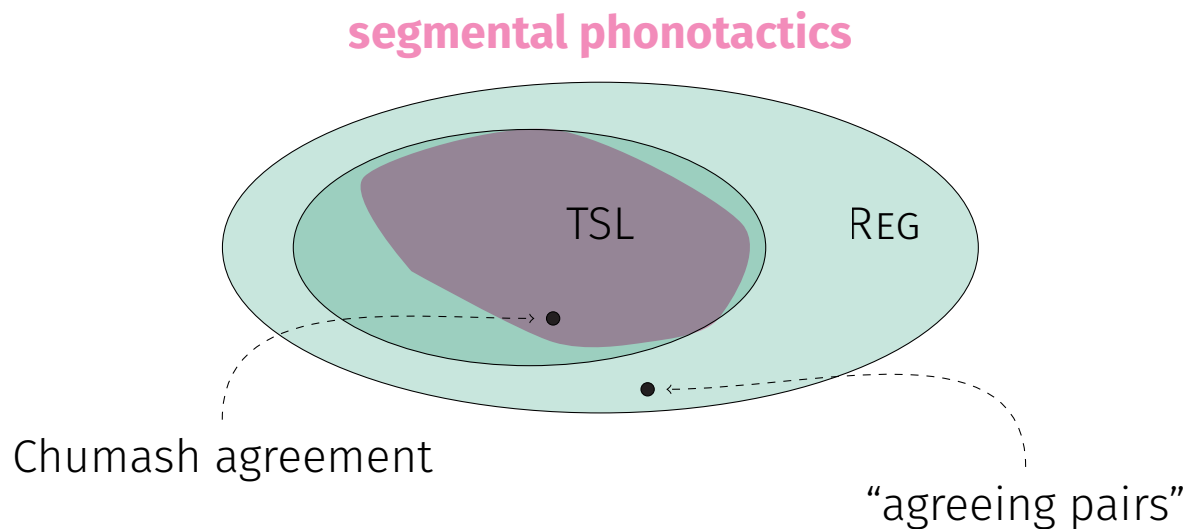
Chumash \* $\int$  with sibilant tier

$\int$   $\int$   
# h a  $\int$  x i n t i l a w a  $\int$  # 'his former Indian name'

s  $\int$  X  
# h a s x i n t i l a w a  $\int$  # (ill-formed)



# Tier-based strictly local sets



- Tier-projection is the standard for learning long-distance phonotactics (Hayes and Wilson, 2008; Jardine and Heinz, 2016; Jardine and McMullin, 2017; Gallagher and Wilson, 2018; McMullin and Hansson, 2019; Gouskova and Gallagher, 2020)

## Challenges for TSL in tone

- Tone has local and non-local patterns that are not TSL
- Two examples:
  - Prinmi (Ding, 2006; Hyman, 2009)
  - Unbounded tone plateauing (Hyman, 2011; Jardine, 2016)
- For more see [Jardine \(2019, to appear\)](#)

## Challenges for TSL in tone

- Prinmi (Ding, 2006):
  - Exactly one H span per word
  - H span can be one or two moras

bí <sup>1</sup> b <sup>1</sup> ob <sup>1</sup> oge	‘as for roasted flour with honey’	HLLL
bí <sup>1</sup> íp <sup>1</sup> ɜtsi	‘sunflower’	HHLL
tʃ <sup>1</sup> in <sup>1</sup> ǎdzjẽɹə	‘dog-nose groups’	LHLL
tõp <sup>1</sup> úm <sup>1</sup> ɜ̀le	‘donkey tail’	LHHL
dʒjõdzim <sup>1</sup> ɜ̀le	‘buffalo tail’	LLHL
ɹətʃi <sup>1</sup> fõ <sup>1</sup> gé	‘as for clean liquor’	LLHH
		*LLLL
		*HLLH
		*LHHH

## Challenges for TSL in tone

- Tier projections cannot distinguish spans of H

\*HH

~~X~~ H H  
 # H L H L # (ill-formed)

~~X~~ HH  
 # L H H L # tōpúmǎle 'donkey tail'

- Prinmi is not TSL

## Challenges for TSL in tone

- Unbounded tone plateauing (UTP) in Luganda

(Hyman and Katamba, 2010; Hyman, 2011)

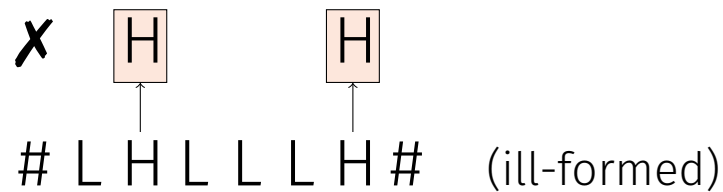
- At most one H span per word
- H span can be of any length

'book'	kitabó	LLL
'chopper'	muté <sup>́</sup> ma	LHL
'log'	kisikí	LLH
'log chopper'	muté <sup>́</sup> má+bí <sup>́</sup> síkí	LHHHHH
	*muté <sup>́</sup> ma+bisikí	*LHLLLH

# Challenges for TSL in tone

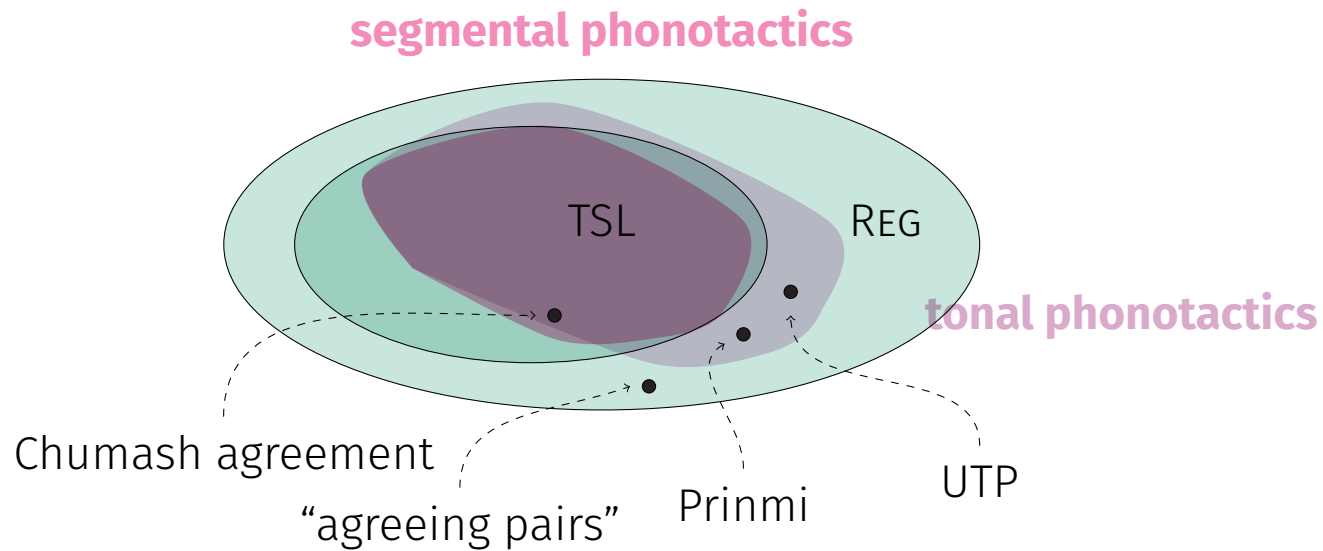
- Tier projections cannot distinguish spans of H

\*HH



- UTP is also not TSL

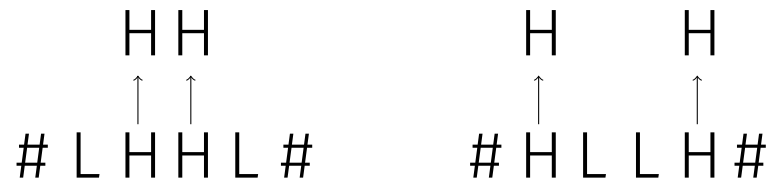
# Challenges for TSL in tone



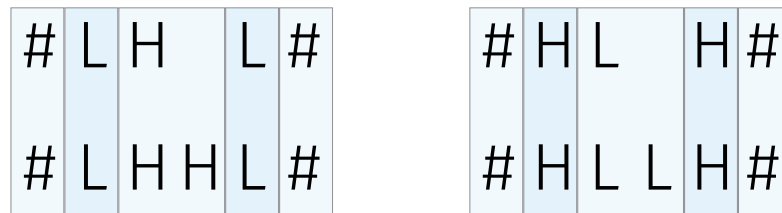
- Other non-TSL patterns: Copperbelt Bemba (Bickmore and Kula, 2015), several accent patterns in Japanese dialects (Haraguchi, 1977), Karanga Shona (Hewitt and Prince, 1989)

# Melody-local sets

- Tier-projection cannot distinguish *spans* of associated TBUs



- Autosegmental **melodies** can (Leben, 1973; Williams, 1976; Goldsmith, 1976)





## Melody-local sets

- **Melody-local (ML)** sets are local over
  - the melody; **and**
  - the string of surface TBUs

(Jardine, to appear)

# Melody-local sets

- UTP:
  - melody: \*HLH
  - string: (none)

**X** # L 

H	L	H
---	---	---

 #  
# L H L L L H # \*mutéma+bisikí

✓ # L H #  
# L H H H H H # mutémá+bisikí 'log chopper'

# Melody-local sets

• Prinmi:

– melody: \*HLH

– string: \*HHH

✓ # L H L #  
# L H H L #

tõpúm<sup>3</sup>ɛ 'donkey tail'

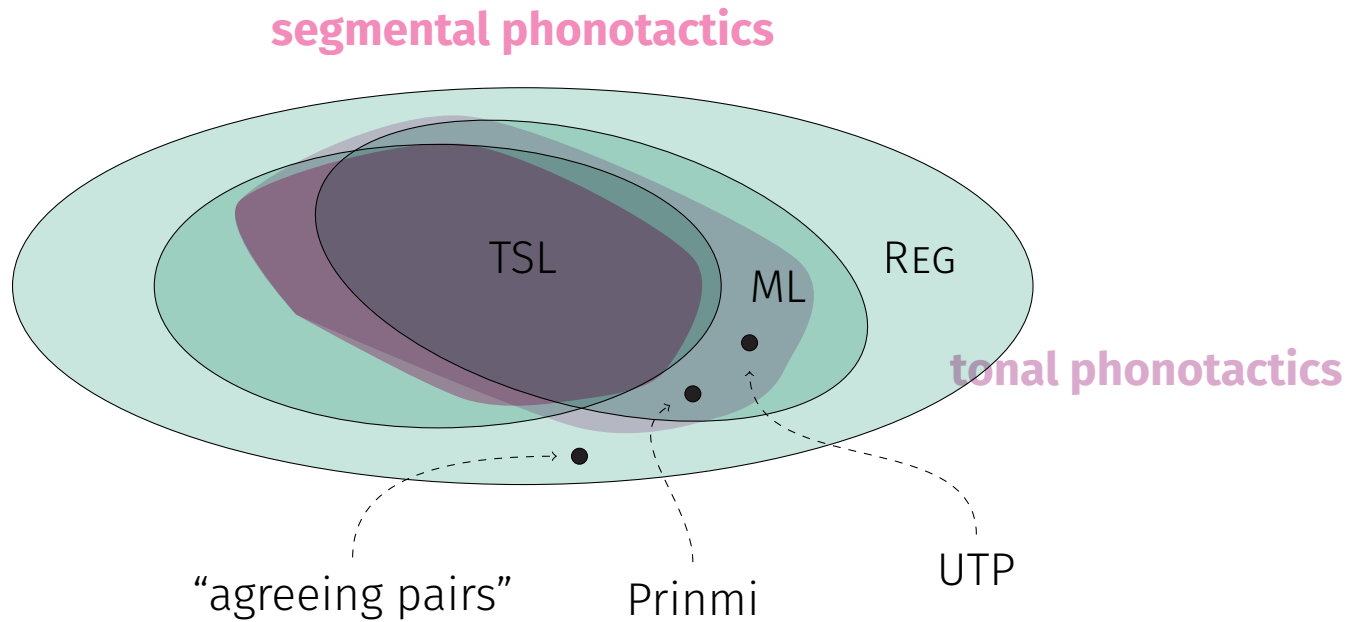
✗ # H L H #  
# H L L H #

\*HLLH

# L H #  
✗ # L H H H #

\*LHHH

# Melody-local sets



- ML sets capture interactions in local and non-local phonotactics in tone, and they are learnable (Jardine, to appear)

# **Tonal processes and input-melody local functions**

## Subsequentiality and phonology

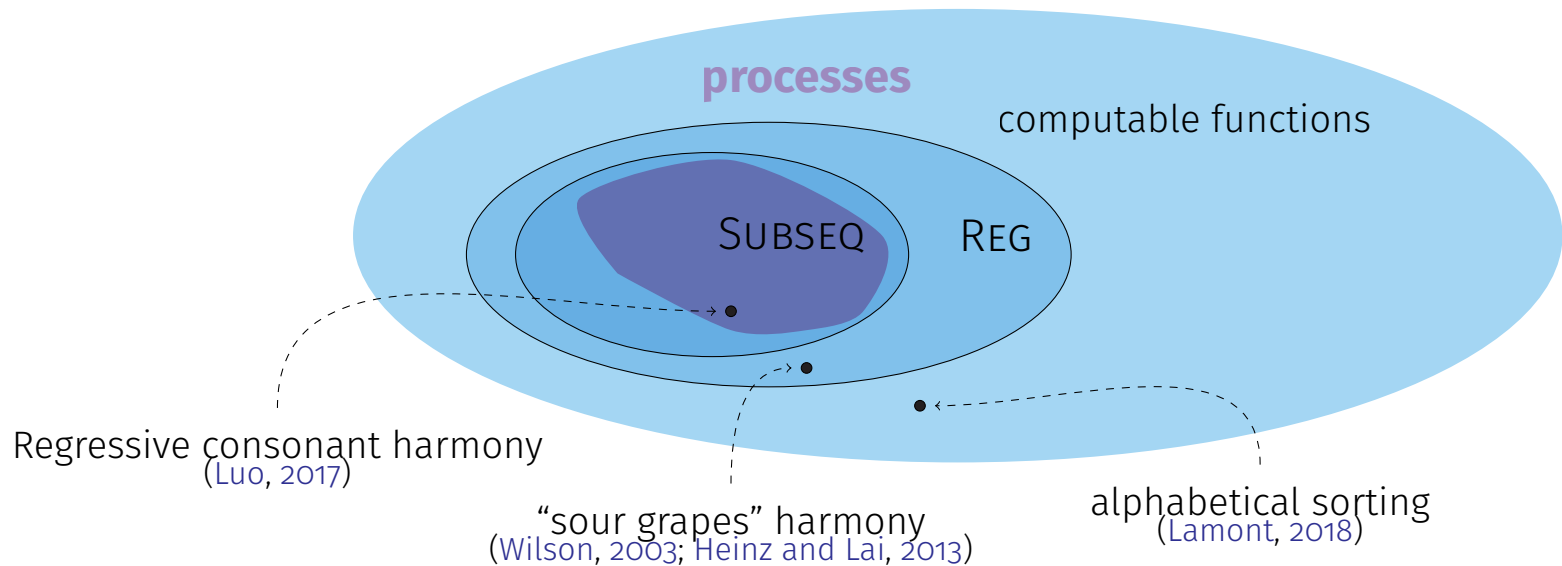
- Phonological patterns are also often considered as **processes**
- A process is a **function** from underlying representation and surface representations

UR	SR	
/s-api-tʃ <sup>h</sup> ol-it/	→ [ʃ-api-tʃ <sup>h</sup> ol-it]	‘I have a stroke of good luck’
/s-api-tʃ <sup>h</sup> ol-us/	→ [s-api-ts <sup>h</sup> ol-us]	‘he has a stroke of good luck’

Inseño Chumash ([Applegate, 1972](#))

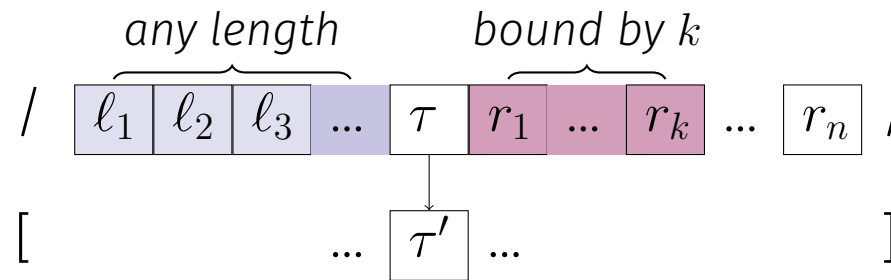
# Subsequentiality and phonology

- Hypothesis: phonological processes are **subsequential functions** (Heinz and Lai, 2013; Payne, 2017; Luo, 2017)



# Subsequentiality and phonology

- Subsequential: output can be determined deterministically in one direction



- (Deterministic  $\neq$  no optionality; Heinz in progress)
- This aligns with Wilson's law that harmony is **myopic**

(Wilson, 2003, 2006; Kimper, 2012)



# Subsequentiality and phonology

- **‘Sour grapes’ (SG) harmony**: spread only when conditions are right on both sides of a target (Wilson, 2003, 2006)

$$\begin{array}{ccc} & \text{UR} & \text{SR} \\ / \text{ s } \dots \underline{\text{s}} \dots \underline{\text{s}} \dots \int / & \rightarrow & [ \text{ s } \dots \underline{\text{s}} \dots \underline{\text{s}} \dots \int ] \\ / \int \dots \underline{\text{s}} \dots \underline{\text{s}} \dots \int / & \rightarrow & [ \int \dots \underline{\int} \dots \underline{\int} \dots \int ] \end{array}$$

- SG is not subsequential (Heinz and Lai, 2013)
- Subsequentiality of segmental phonology is well-supported (Heinz and Lai, 2013; Luo, 2017; Payne, 2017, though c.f. McCollum et al. 2017)
- Subsequential functions are learnable (Oncina et al., 1993; Jardine et al., 2014; Chandlee et al., 2015)

## Subsequentiality and tone

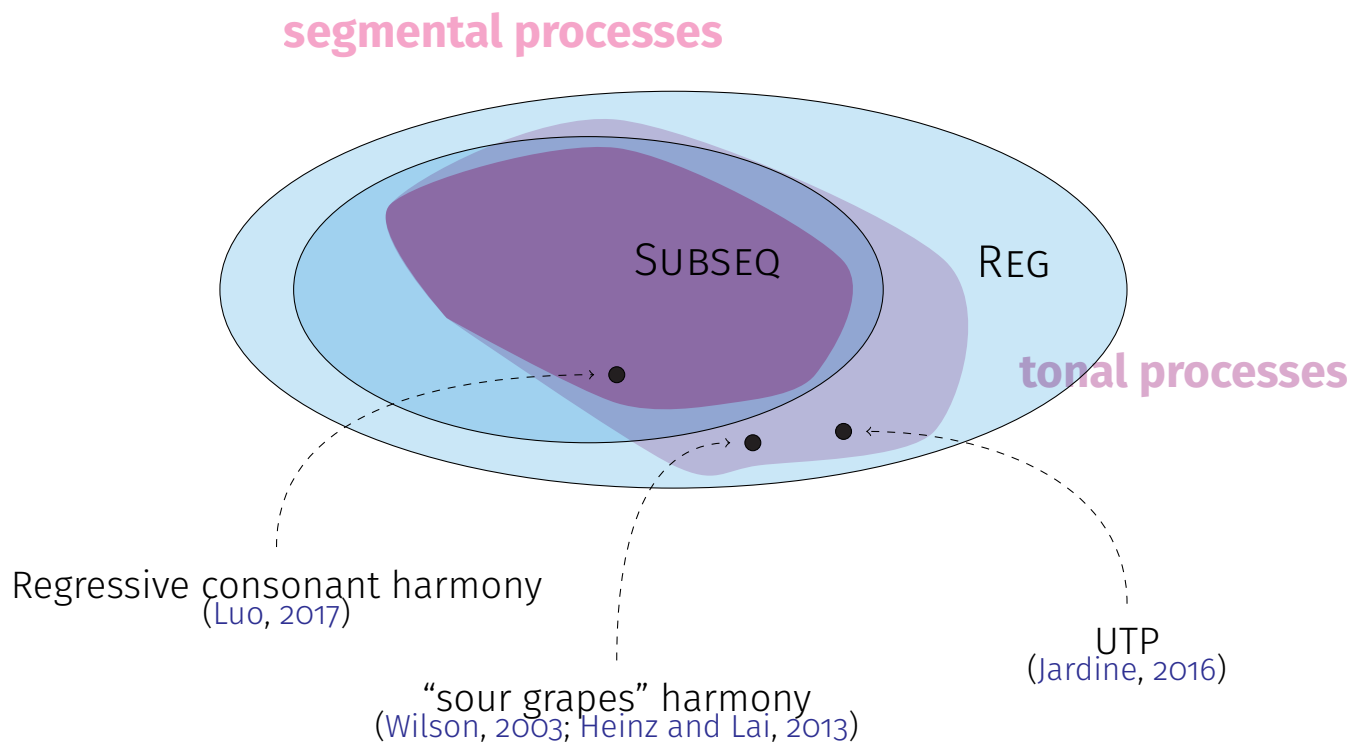
- However, UTP is like SG

mutéma	/LHL/	→ [LHL]	'chopper'
kisikí	/LLH/	→ [LLH]	'log'
mutémá+bísíkí	/LHLLLH/	→ [LHHHHH]	'log chopper'

(Hyman and Katamba, 2010)

- [Jardine \(2016\)](#): SG-like processes are common in tone

# Subsequentiality and tone



## Input melody-local functions

- ML sets were local over
  - the melody; **and**
  - the string of surface TBUs
  
- Mamadou (in progress) proposes ML **functions** that are local in the same way<sup>2</sup>



# Input melody-local functions

# L H L H #

# L H L L L H #

/mutéma+bisikí/

UR

#

#

SR

# Input melody-local functions

# L H L H #

# L

# L H L L L H #

# L

/mutéma+bisikí/

UR

SR

# Input melody-local functions

# L H L H #

# L H L L L H #

/mutéma+bisikí/

UR

# L H

# L H

SR

# Input melody-local functions

# L H L H #

# L H L L L H #

/mutéma+bisikí/

UR

# L H

# L H

SR



# Input melody-local functions

# L H L H #

# L H L L L H #

/mutéma+bisikí/

UR

# L H

# L H

SR

# Input melody-local functions

# L H L H #

# L H L L H #

/mutéma+bisikí/

UR

# L H

# L H H

SR

# Input melody-local functions

# L H L H #

# L H L L L H #

/mutéma+bisikí/

UR

# L H

# L H H H

SR

# Input melody-local functions

# L H L H #

# L H L L L H #

/mutéma+bisikí/

UR

# L H

# L H H H H

SR

# Input melody-local functions

# L H L H #

# L H L L L H #

/mutéma+bisikí/

UR

# L H

# L H H H H H

SR

# Input melody-local functions

# L H L H #

# L H L L L H #

/mutéma+bisikí/

UR

# L H                    #

# L H H H H H #

SR

# Input melody-local functions

# L H L H #

# L H L L L H #

/mutéma+bisikí/

UR

# L H                    #

# L H H H H H #

[mutémá+bísíkí]

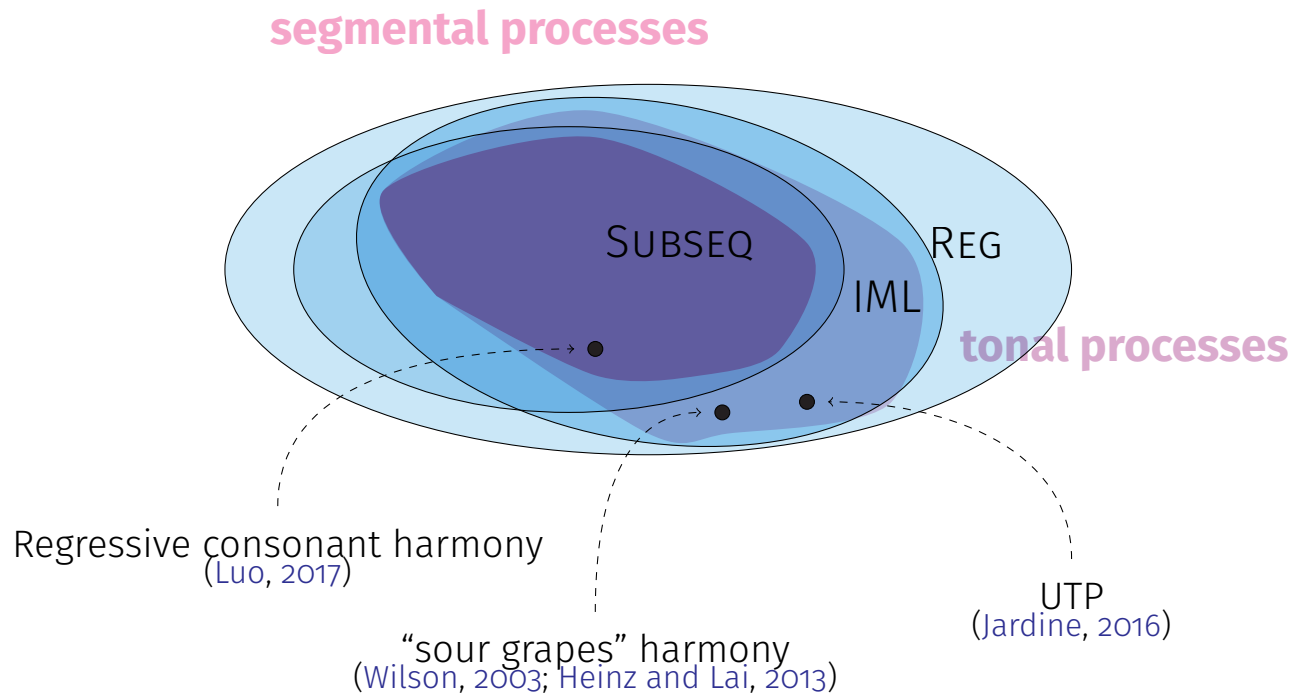
SR

## Input melody-local functions

- UTP is deterministic **when considering the melody**
- In fact, it is local



# Input melody-local functions

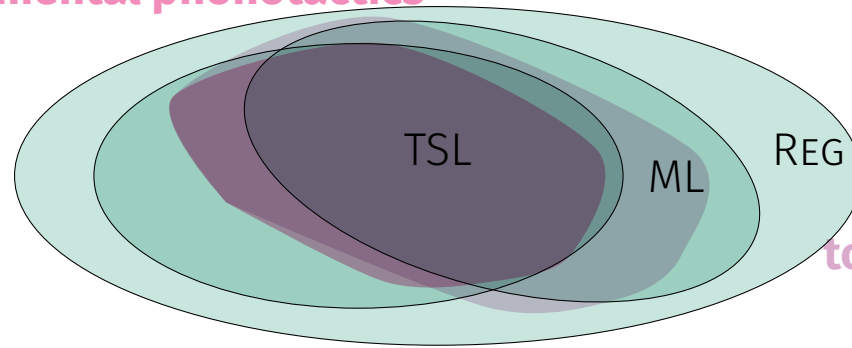


- Mamadou (in progress): IML is a good fit for tonal processes

# Discussion

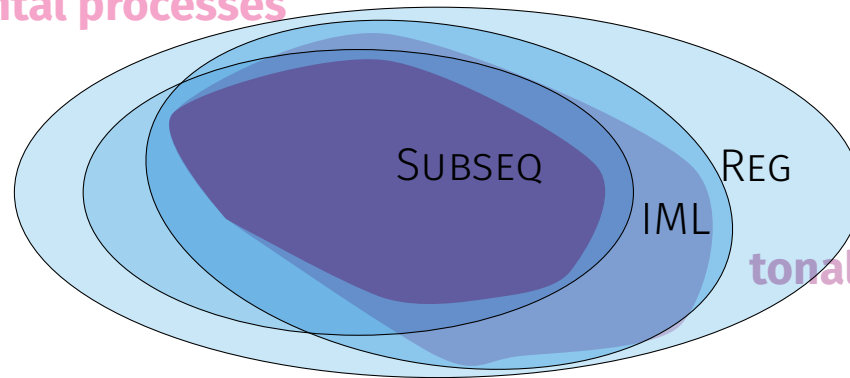
# Discussion

segmental phonotactics



tonal phonotactics

segmental processes



tonal processes

## Discussion

Hyman (2011): “[T]one can do everything that segmental and metrical phonology can do, but the reverse is not true.”

- The computational perspective helps explain difference between segmental phonology and tone
- **Melody** representation is key to difference
- Computational **locality** is preserved
- For ML sets, this also guarantees learnability

## Future work

- Learnability of IML functions can be studied using subsequential learning techniques
- Hypothesis: ML/IML are the “outer limits” of what are possible in phonology
- How do IML functions compare to local autosegmental functions?  
(Chandlee and Jardine, 2019)

# Thank you!

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