

Overview

- Computational characterizations of phonology lead to restrictive, testable, and learnable theories of phonological processes (Heinz, 2018).
- Research question: what kind of maps are tone mapping patterns?
- $\mathrm{mo}\,\mathrm{e}\,\mathrm{re}\,\mathrm{ka}\,\mathrm{\eta}\mathrm{ge}\,\mathrm{ri}\,\mathrm{e} \quad \rightarrow \quad \mathrm{mo}\,\mathrm{e}\,\mathrm{re}\,\mathrm{ka}\,\mathrm{\eta}\mathrm{ge}\,\mathrm{ri}\,\mathrm{e}$

- LHLH
 - L HL H (Kikuyu; Clements and Ford 1979)
- **Result**: Maps defined with quantifier-free least fixed point logic give a restrictive, **output-local** characterization of tone mapping patterns

Logical maps

• Logical formulas define outputs through properties of the input (Courcelle, 1994)

$$c(x) \stackrel{\text{def}}{=} b(x) \wedge a(p(x))$$

 $a \stackrel{p}{\leftarrow} b \mapsto a \stackrel{p}{\leftarrow} c$

• Tone mapping defines association

 $\mu \mu$ A(x, y) \mapsto TT TT

- These definitions
 - are quantifier free (Chandlee and Lindell, forthcoming)
 - use least fixed point operators (Libkin 2004), which allow recursive definitions (shown here with *implicit definitions*; Rogers 1997)
 - Use *either* predecessor (*p*) or successor (*s*)

Analyses

Mende (Left-to-right) $R(x, y) \stackrel{d}{=} \underbrace{(first(x) \land first(y))}_{inverse}$	()) $\vee (R(p(x), p(y)))$	$\lor (last(y) \land$	R(p(x), y))		A
# µ	μμ	μ μ		$\mu \mu \mu \mu$	μ
# T	TT	T #		LHL	L
(a)	(b)	(c)		(a)	
Kikuyu (1st tone to 1st and 2nd TBUs; then left-to-right) $R(x, y) \stackrel{d}{=} (b) \lor (c) \lor (first(y) \land second(x))$				A(x, y)	<u>d</u>
	# µ µ	$ \begin{array}{ccc} \mu \mu \mu \mu \mu \mu \\ \downarrow \\ \downarrow$		$\mu \mu \mu \mu \mu \mu$	
	# T	H LH H LH			
Hausa (Right-to-left)	(d)	(a)	(d)	(b)	
$R(x,y) \stackrel{\mathrm{d}}{=} \underbrace{\left(last(x) \land last(y)\right)}_{\checkmark}$	$\vee \underbrace{\left(R(s(x), s(y))\right)}_{\checkmark} \vee$	$\underbrace{(first(y) \land x)}_{\bullet}$	R(s(x), y))		
μ #	μ μ	μ μ		$\mu \mu \mu \mu$	I
T #	TT	# T		L HL]
(e)	(f)	(g)		(e)	

Discussion

- Begins solution for problem of logical complexity of tone mapping Jardine (2017)
- A principled characterization of the range of possible tone association patterns
- Can capture patterns that cannot be captured by OT ALIGN constraints
- Explains absence of unattested patterns, like centering:

• Recursive definitions provide the first logical definition of output-based locality for phonology

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