Subregular Learning of a Phonology and a Set of Underlying Forms

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Introduction

UR and Phonological grammar learning

- **Learning problem:** the simultaneous inference of underlying representations (URs) and a phonological grammar from alternating surface representations (SRs)

  (Merchant, 2008; Tesar, 2014; Cotterell et al., 2015)

- **Our proposal:** a solution based on the structure provided by the input strictly local (ISL) functions

  (Chandlee and Heinz, 2018; Jardine et al., 2014)

English plural

The plural morpheme in English has at least two pronunciations: [s] and [z].

Morphemes	SR
CAT-PL	[kætˢ]
CUFF-PL	[kʌfˢ]
DEATH-PL	[dɛθˢ]
GIRL-PL	[gɜ:rlᶻ]
CHAIR-PL	[t͡ʃɛərᶻ]
BOY-PL	[bɔɪᶻ]
...	...

English plural

The plural morpheme in English has at least two pronunciations: [s] and [z].

Analysis:

- A map from morphemes to URs
  - CAT→/kæt/
  - PL→/z/
  - etc.
- A map from URs to SRs
  /z/ → [s] /[-SONORANT] __

Morphemes	SR
CAT-PL	[kæts]
CUFF-PL	[kʌfs]
DEATH-PL	[dɛθs]
GIRL-PL	[gɜ:rlz]
CHAIR-PL	[t͡ʃɛərz]
BOY-PL	[bɔɪz]
...	...

Formalizing the problem

- M: set of morphemes
- Σ: alphabet of symbols in SR and UR (segmental inventory)
- Targets:
  - lexicon function $\ell : M^* \to \Sigma^*$
  - phonology function $\varphi : \Sigma^* \to \Sigma^*$

Formalizing the problem

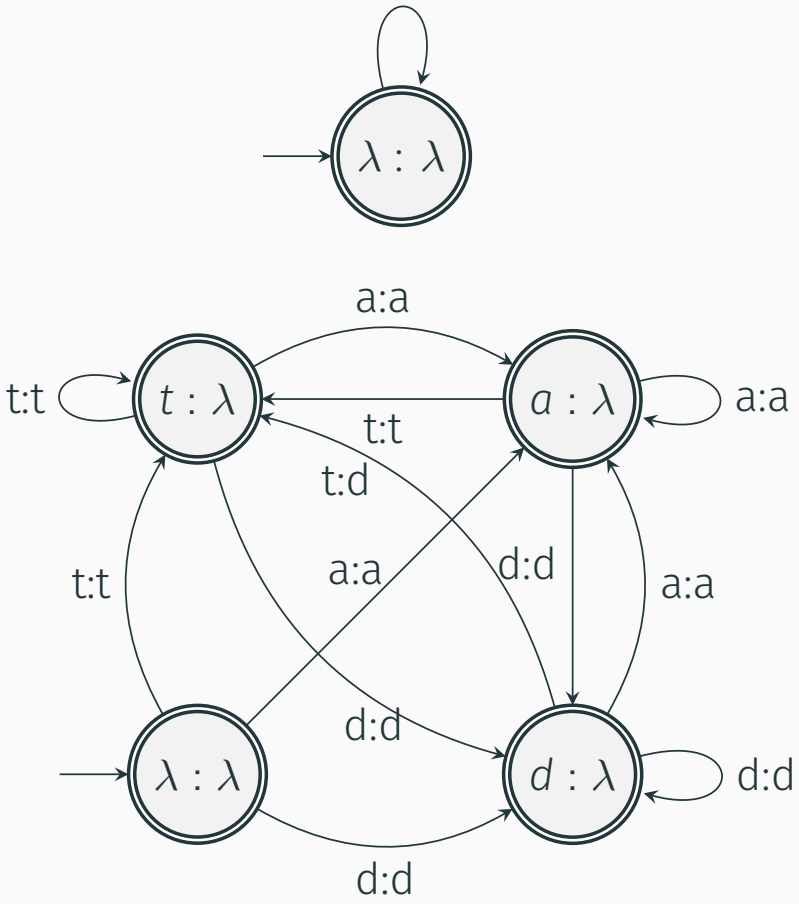
- M: set of morphemes
- Σ: alphabet of symbols in SR and UR (segmental inventory)
- Targets:
  - lexicon function $\ell : M^* \to \Sigma^*$
  - phonology function $\varphi : \Sigma^* \to \Sigma^*$
- Learning data is generated by $\varphi \circ \ell$; i.e., a finite set D such that

$$\forall \langle m, s \rangle \in D, \quad \varphi(\ell(m)) = s$$

- Note: ℓ is an ISL_1 function from morphemes to URs
- ISL functions only make changes in the output with respect to the local information in the input.

Target transducers and learning data

r_1 : /tat/ s_1 : /ta/
r_2 : /tad/ s_2 : /da/
r_3 : /a/ s_3 : /da/



m	s
r_1s_1	[tatta]
r_1s_2	[tatda]
r_1s_3	[tata]
r_2s_1	[tadda]
r_2s_2	[tadda]
r_2s_3	[tada]
r_3s_1	[ata]
r_3s_2	[ada]
r_3s_3	[aa]

Target transducers and learning data

r_1 : /tat/ s_1 : /ta/
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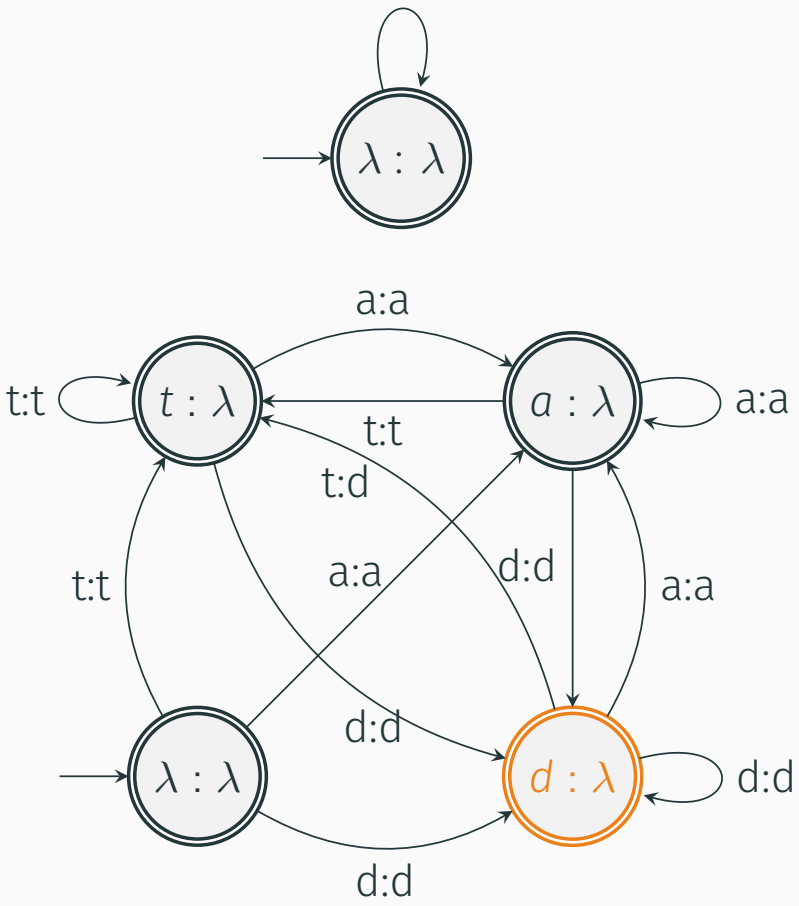

m	s
r_1s_1	[tatta]
r_1s_2	[tatda]
r_1s_3	[tata]
r_2s_1	[tadda]
r_2s_2	[tadda]
r_2s_3	[tada]
r_3s_1	[ata]
r_3s_2	[ada]
r_3s_3	[aa]

Target transducers and learning data

r_1 : /tat/ s_1 : /ta/
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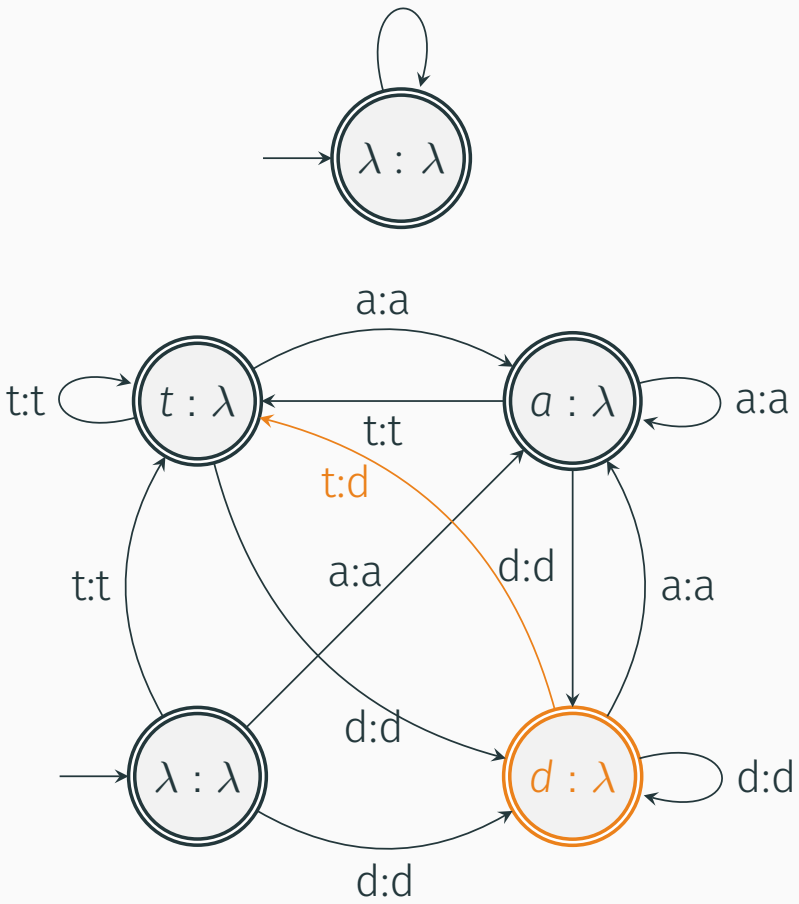

m	s
r_1s_1	[tatta]
r_1s_2	[tatda]
r_1s_3	[tata]
r_2s_1	[tadda]
r_2s_2	[tadda]
r_2s_3	[tada]
r_3s_1	[ata]
r_3s_2	[ada]
r_3s_3	[aa]

Assumptions

The learner knows *a priori*:

- A lexicon of morphemes/lexical meanings (M), in which each morpheme has only one UR (ℓ is ISL_1).
- The ISL_k structure of phonology function. Here, we focus on ISL_2

Proposed Learner

Roadmap

- Initial hypothesis
- Learning procedure

Initial hypothesis

- Initial hypothesis for ℓ: prefix tree transducer T_ℓ, obtained from SR segmentation based on longest common prefix (LCP)

(Oncina et al., 1993; Jardine et al., 2014)

Single Process Example: Initial lexicon transducer

m	s
r_1s_1	[tatta]
r_1s_2	[tatda]
r_1s_3	[tata]
r_2s_1	[tadda]
r_2s_2	[tadda]
r_2s_3	[tada]
r_3s_1	[ata]
r_3s_2	[ada]
r_3s_3	[aa]

LCP of SR is tat

Single Process Example: Initial lexicon transducer

m	s
$r_1 s_1$	[tatta]
$r_1 s_2$	[tatda]
$r_1 s_3$	[tata]
$r_2 s_1$	[tadda]
$r_2 s_2$	[tadda]
$r_2 s_3$	[tada]
$r_3 s_1$	[ata]
$r_3 s_2$	[ada]
$r_3 s_3$	[aa]

LCP of SR is tad

Single Process Example: Initial lexicon transducer

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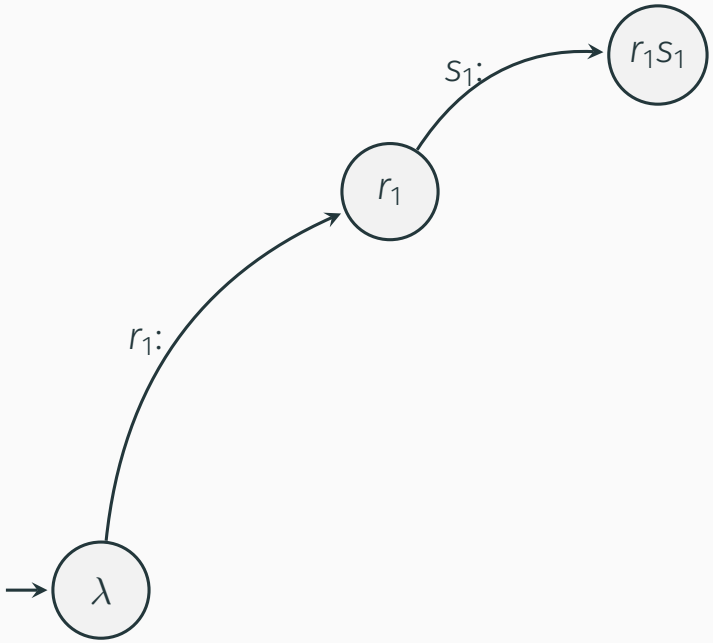
$r_1 s_1$	[tatta]
$r_1 s_2$	[tatda]
$r_1 s_3$	[tata]
$r_2 s_1$	[tadda]
$r_2 s_2$	[tadda]
$r_2 s_3$	[tada]
$r_3 s_1$	[ata]
$r_3 s_2$	[ada]
$r_3 s_3$	[aa]

LCP of SR is a

Single Process Example: Initial lexicon transducer

m	s
$r_1 s_1$	[tatta]
$r_1 s_2$	[tatda]
$r_1 s_3$	[tata]
$r_2 s_1$	[tadda]
$r_2 s_2$	[tadda]
$r_2 s_3$	[tada]
$r_3 s_1$	[ata]
$r_3 s_2$	[ada]
$r_3 s_3$	[aa]



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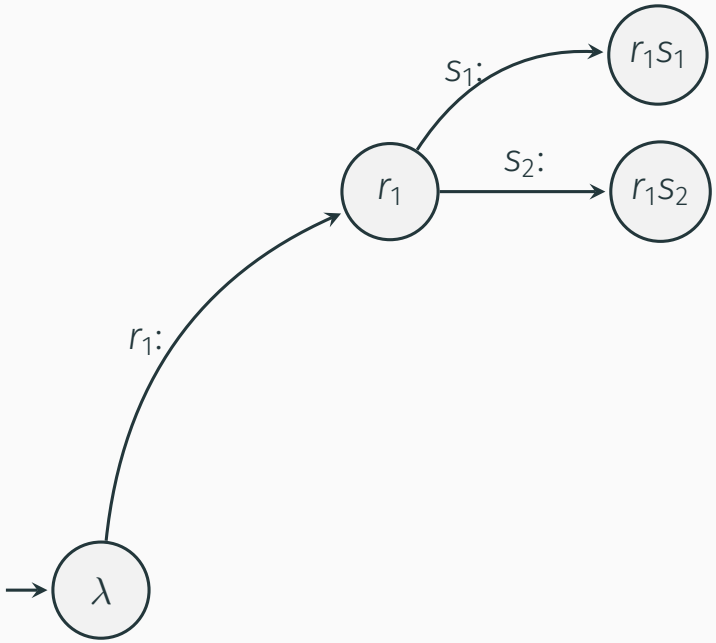
r_1s_3	[tata]
r_2s_1	[tadda]
r_2s_2	[tadda]
r_2s_3	[tada]
r_3s_1	[ata]
r_3s_2	[ada]
r_3s_3	[aa]



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r_1s_3	[tata]
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r_2s_2	[tadda]
r_2s_3	[tada]
r_3s_1	[ata]
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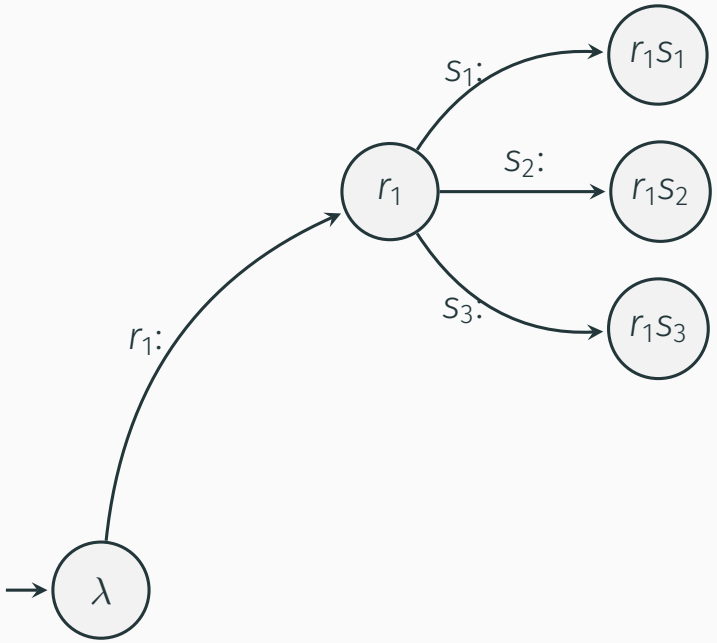
r_3s_3	[aa]



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r_2s_1	[tadda]
r_2s_2	[tadda]
r_2s_3	[tada]
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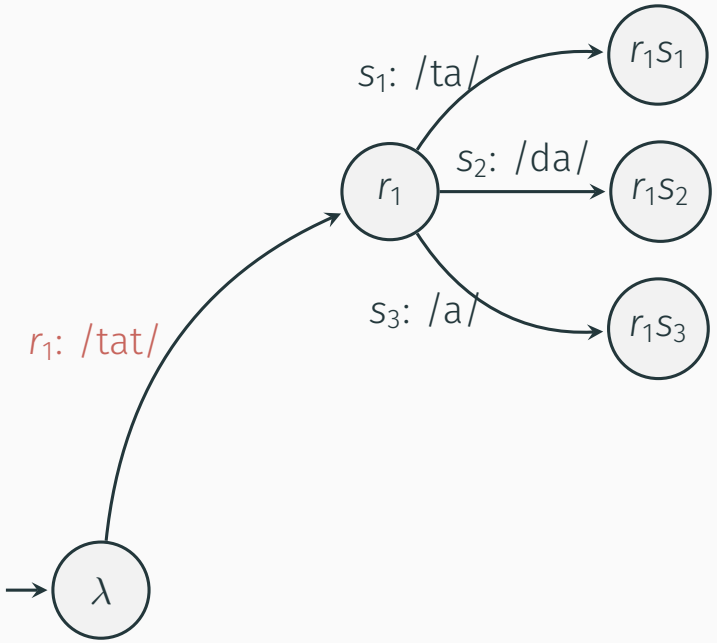
r_3s_3	[aa]



Single Process Example: Initial lexicon transducer

m	*s*
r_1s_1	[tatta]
r_1s_2	[tatda]
r_1s_3	[tata]
r_2s_1	[tadda]
r_2s_2	[tadda]
r_2s_3	[tada]
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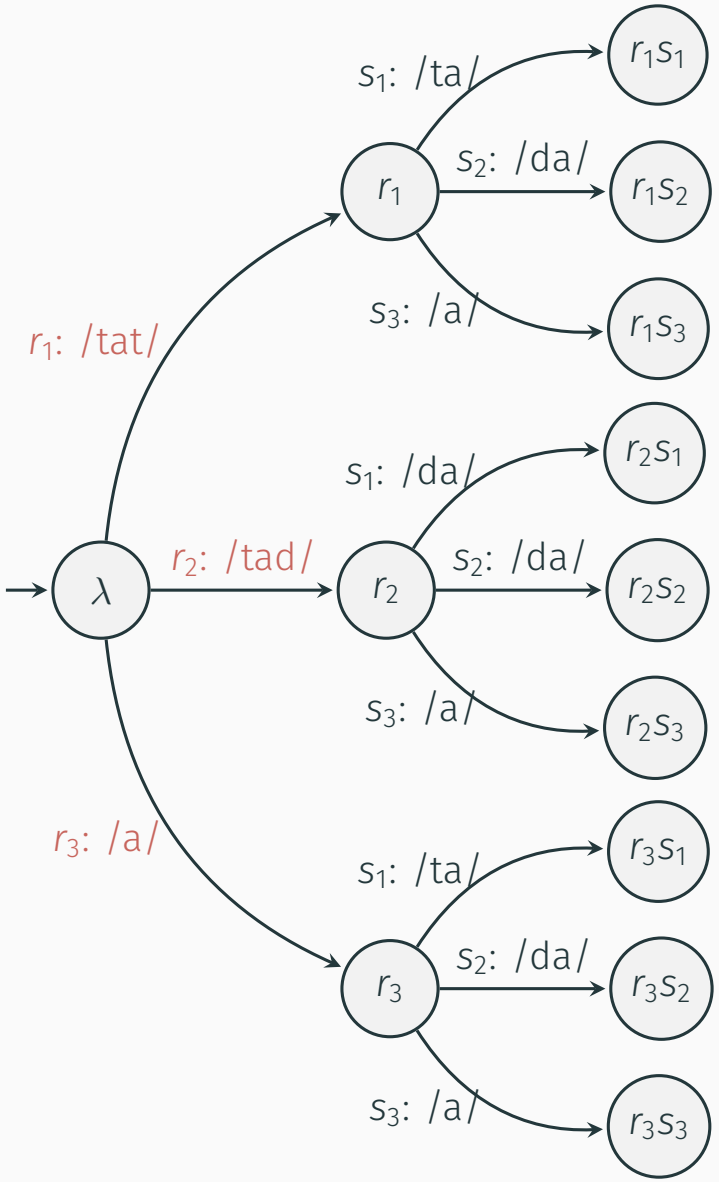


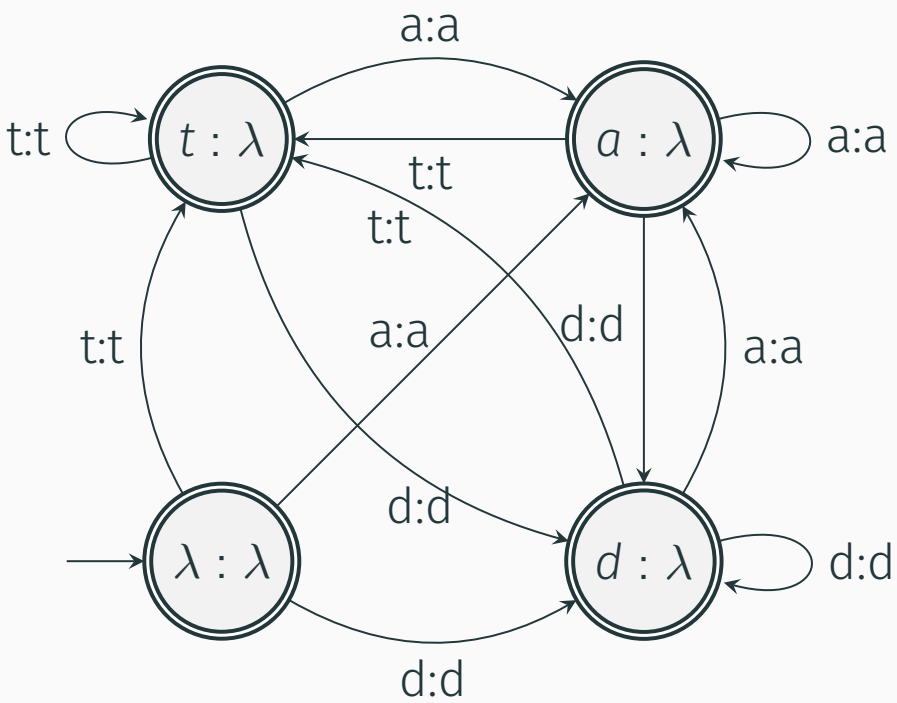
Initial hypothesis

- Initial hypothesis for ℓ: prefix tree transducer T_ℓ, obtained from SR segmentation based on longest common prefix

  (Oncina et al., 1993; Jardine et al., 2014)

- Initial hypothesis for φ: ISL_2 transducer T_φ for identity function

Single Process Example: phonology transducer



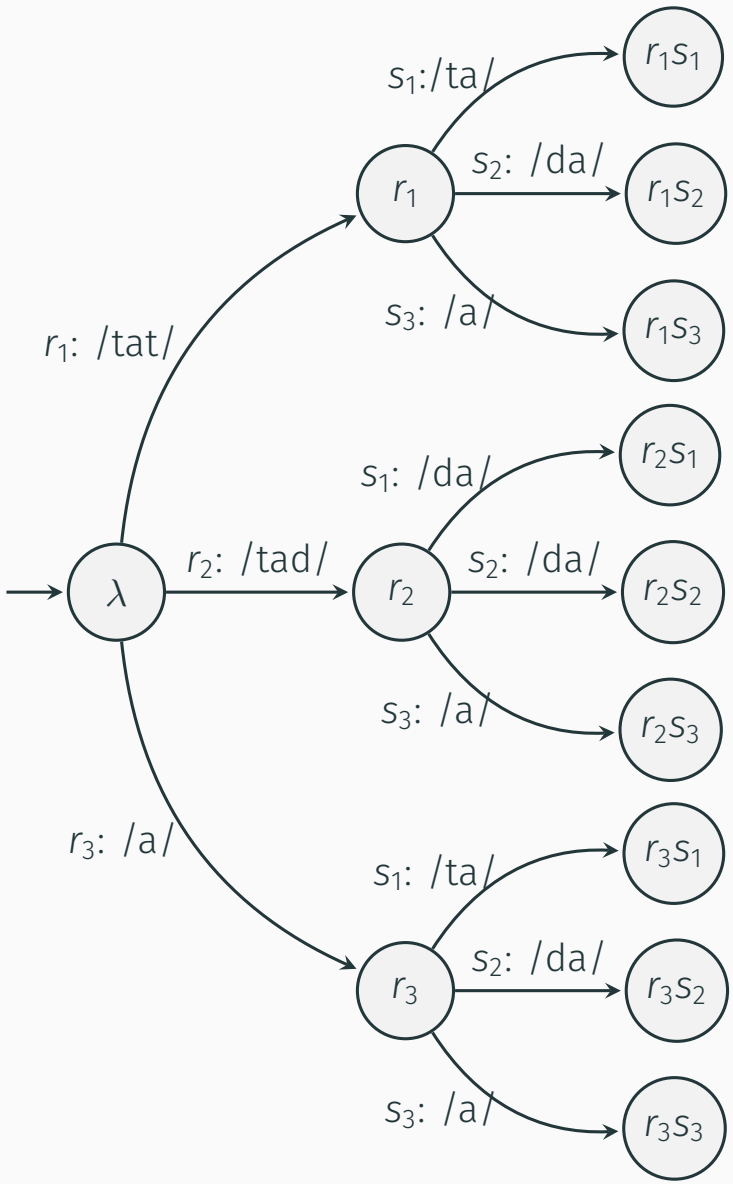
Identity function:
/tadt/→[tadt]
/tatt/→[tatt]
. . .

Learning Procedure

- Modify lexicon transducer T_ℓ until one UR per morpheme
- For each change in lexicon transducer T_ℓ, make *opposite* change in phonology transducer T_φ

Inconsistency detection

The learner detects the inconsistency on lexicon transducer T_ℓ



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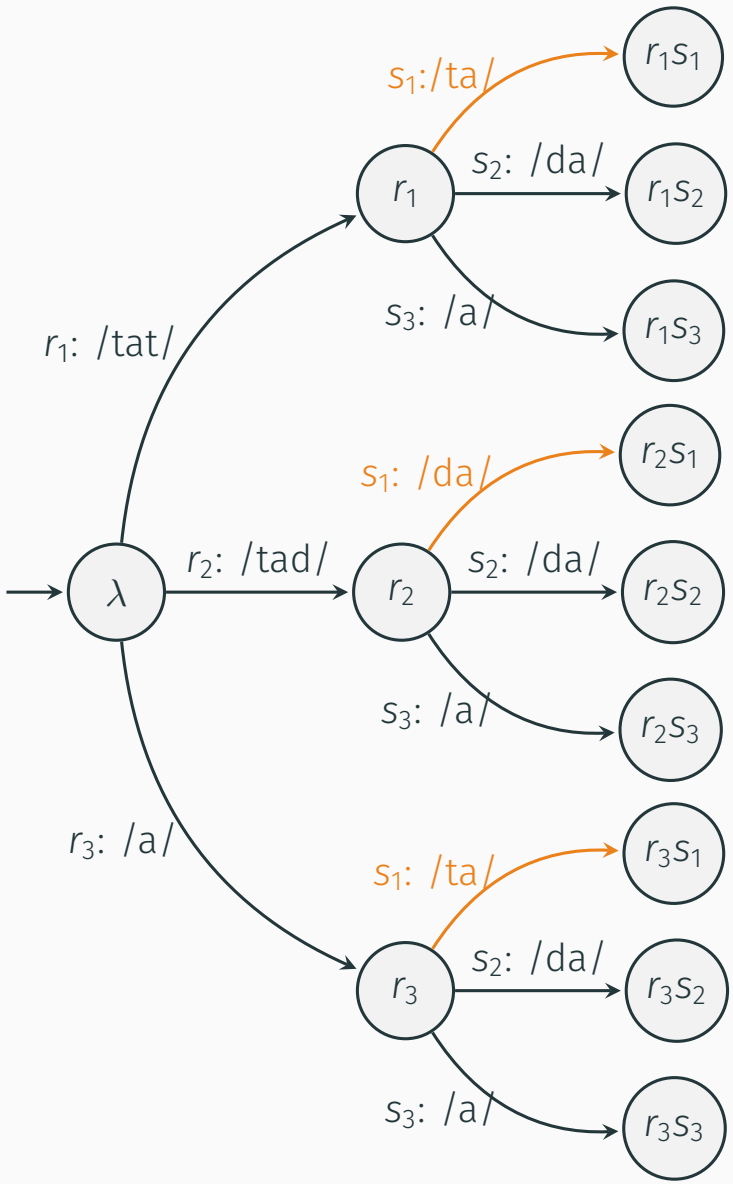
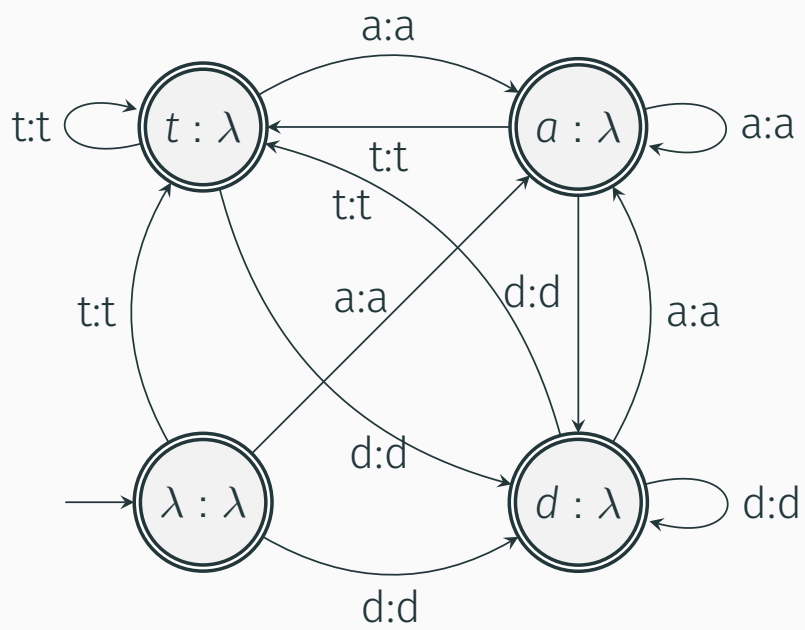
The learner detects the inconsistency on lexicon transducer T_ℓ



Environment Collection

Find environment for different SRs based on the phonology transducer.



environment	s_1

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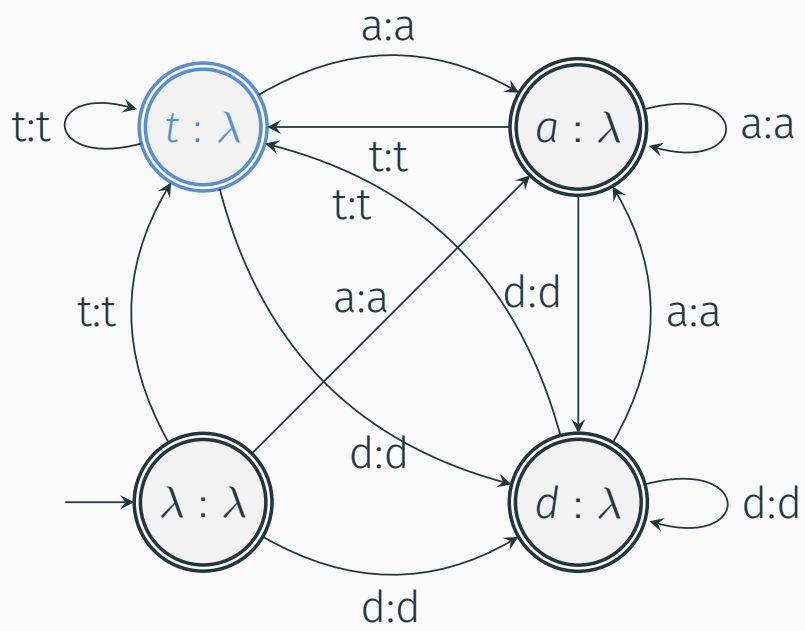

	environment	s_1
$r_1 s_1$	tat	ta

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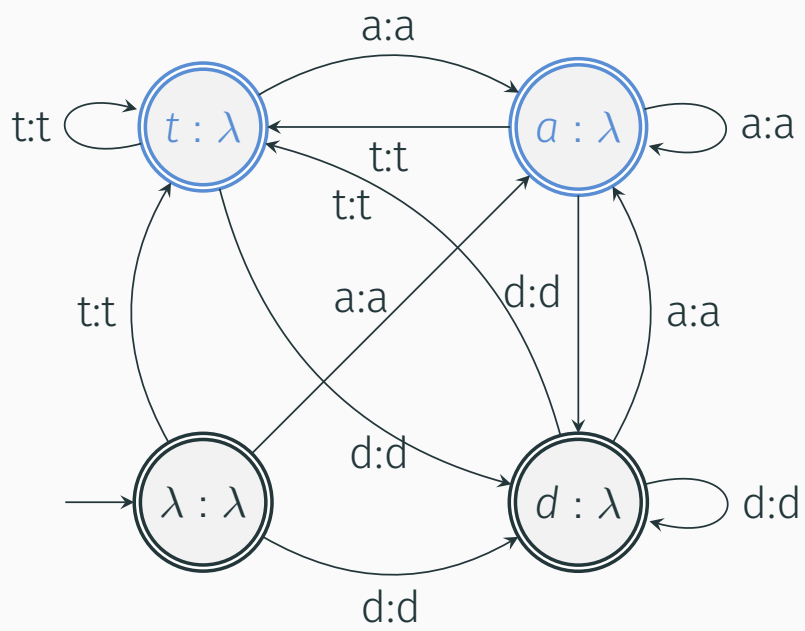

	environment	s_1
$r_1 s_1$	tat	ta
$r_3 s_1$	a	ta

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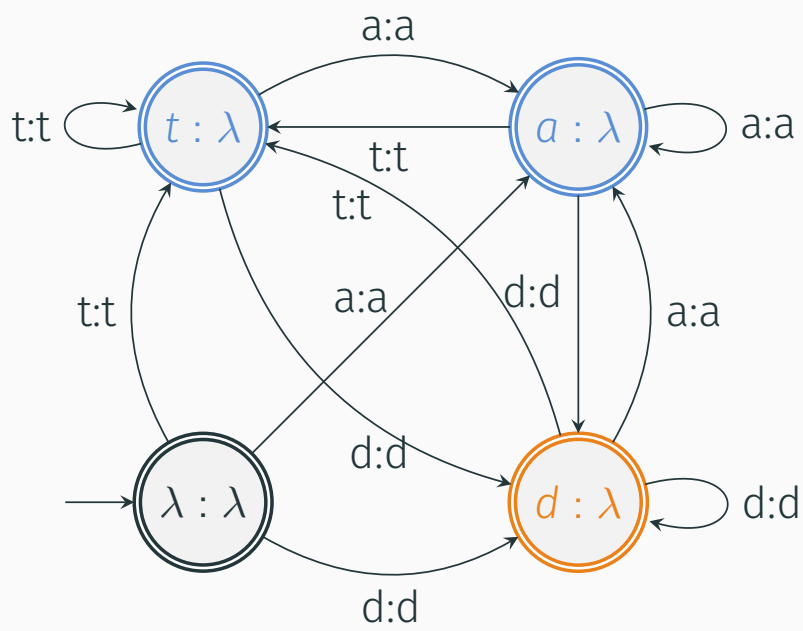
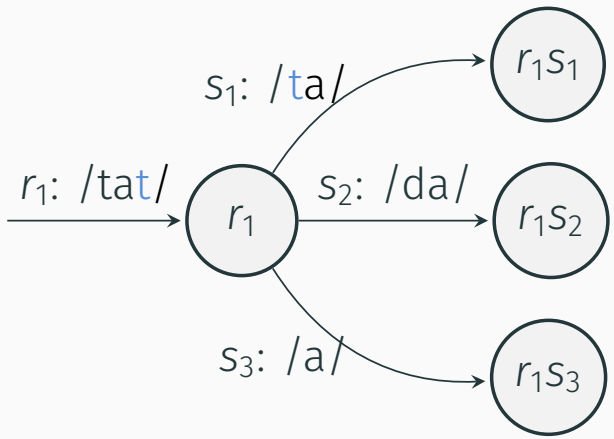
Find environment for different SRs based on the phonology transducer.

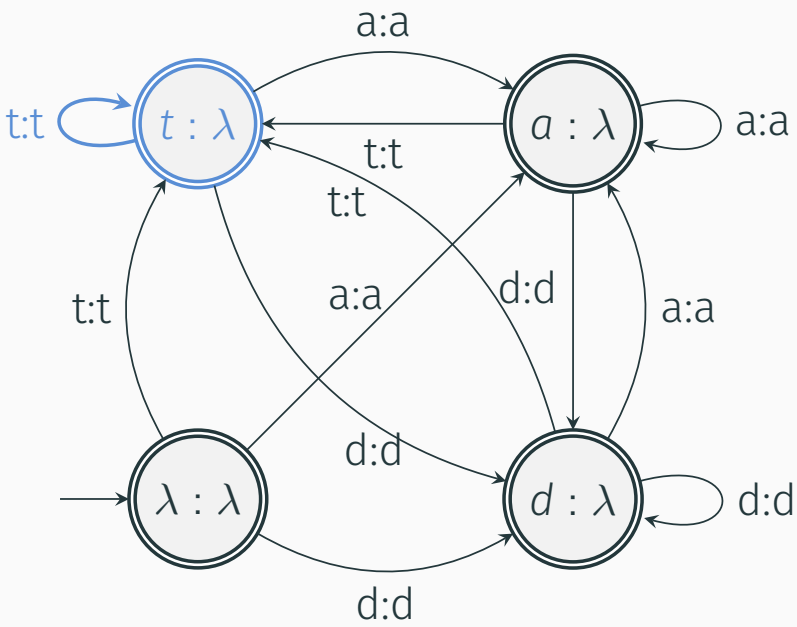


	environment	s_1
$r_1 s_1$	tat	ta
$r_3 s_1$	a	ta
$r_2 s_1$	tad	da

Modifying Transducers

Change SR into UR in the prefix-tree transducer.
Make an opposite change in the phonology transducer.





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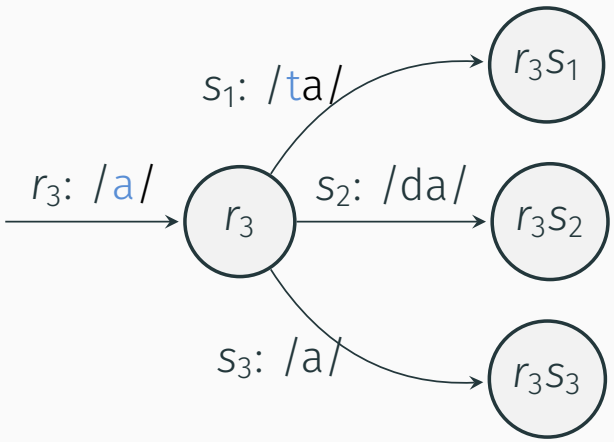
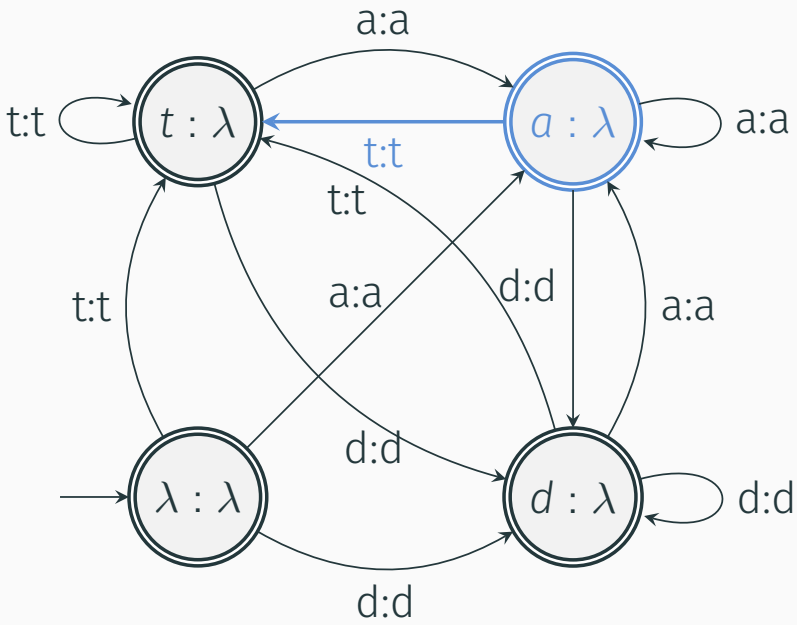
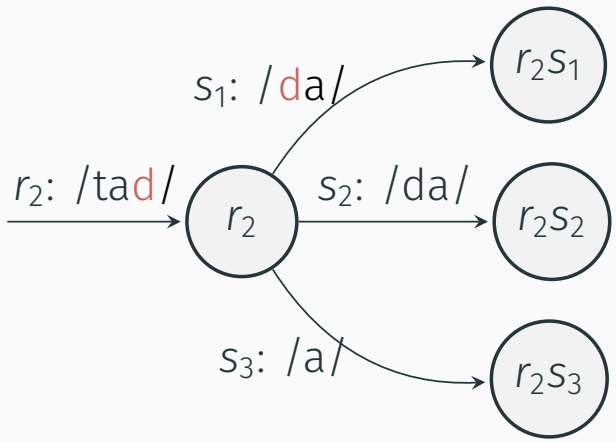
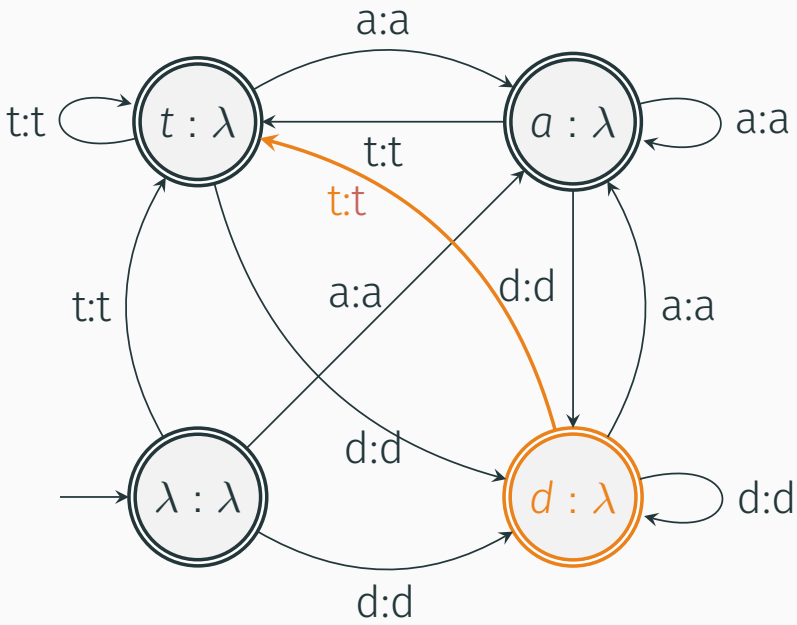




Modifying Transducers

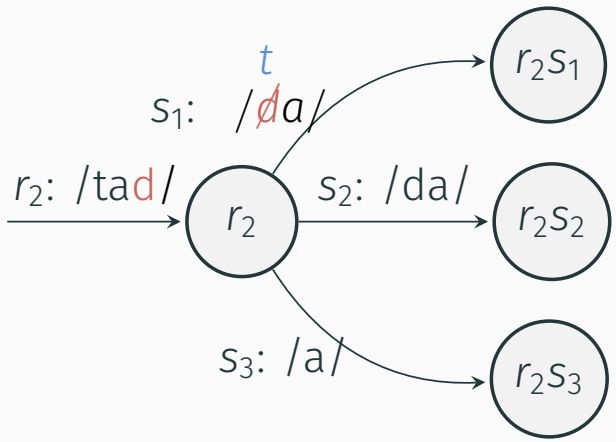
Change SR into UR in the prefix-tree transducer.
Make an opposite change in the phonology transducer.

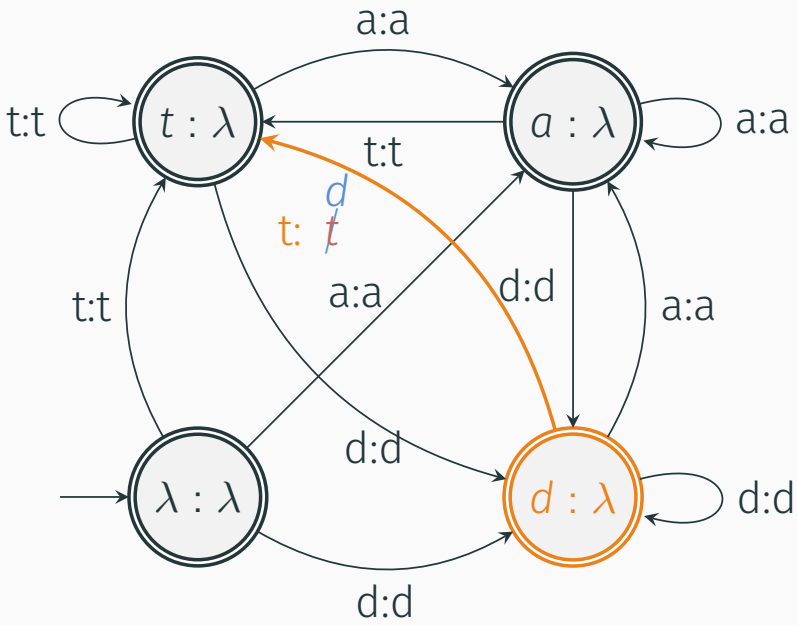




Modifying Transducers

Change SR into UR in the prefix-tree transducer.
Make an opposite change in the phonology transducer.





Primary Result

- The learner can learn assimilation, dissimilation, deletion, epenthesis and metathesis.
- So far it learns only one phonology process from a data set.
- In particular, it is able to learn opacity, *i.e.* self-counter-feeding and self-counter-bleeding.

Future Research

- Learn multiple phonology processes simultaneously from one data set.
- Learn all ISL_2 functions.
- Learn all ISL_k functions for any given k.
- Learn Output-Strictly-Local (OSL) phonology transformations.

  (Chandlee et al., 2015).
- ...

Discussion

Three questions

- Why we design an ISL learner, *i.e.* why not OSL learner or Output Tier Based Strictly Local (OTSL) learner?

  (Chandlee et al., 2015; Burness and McMullin, 2019)

- How abstract is the learnt UR? Specifically, is it able to learn abstract URs?

  (Kiparsky, 1968; Kenstowicz and Kisseberth, 2014)

- What differentiate subregular learners from other learners?

Why ISL phonology?

- Empirically significant: 94% of phonology patterns in P-Base database are ISL.

  (Mielke, 2004; Chandlee and Heinz, 2018).

- Learning based on the structure of ISL class can be extended to OSL and OTSL functions, which both share a particular structure

Can we learn abstract URs?

- It depends.

Can we learn abstract URs?

- It depends.
- Two cases: whether the abstract UR exerts phonological influence on the target phonology function.

Subregular learner *vs.* Other learners

- Current learner: **specific to learning phonology**.

  (Gallistel and King, 2011; Heinz, 2010).

- Cue-based parameter setting model and Learners based on Optimality Theory: **non-specific to learning phonology**

  (Dresher and Kaye, 1990; Dresher, 1999; Jarosz, 2006; Apoussidou, 2007; Merchant, 2008; Merchant and Tesar, 2008).

Subregular learner *vs.* Other learners

- Current learner: **specific to learning phonology**.

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- Cue-based parameter setting model and Learners based on Optimality Theory: **non-specific to learning phonology**

  (Dresher and Kaye, 1990; Dresher, 1999; Jarosz, 2006; Apoussidou, 2007; Merchant, 2008; Merchant and Tesar, 2008).

- Modular learning: an ISL learner is an independent module in learning the whole phonology. By composing different modules, the knowledge of the whole is acquired.

  Heinz (2010, 2011).

Conclusion

Summary

- Subregular classes of functions provide structure for the simultaneous induction of URs and the phonological grammar
- The general procedure here can be extended to learning iterative (output-based) processes, long-distance processes, and process interactions

Acknowledgements

We thank Bruce Tesar, Adam McCollumn, Mariapaola D'imperio, Colin Wilson, Eric Baković, Chris Oakden, Dine Mamadou, Jill Harper, Sreekar Raghotham, the Rutgers MathLing group, and the audience at the Rutgers/SBU/Haverford/Delaware subregular phonology workshop, for their insightful comments.

Backup slides

Regressive Assimilation

/t/ becomes voiced [d] before /d/.

m	*s*
r_1s_1	[tatta]
r_1s_2	[tadda]
r_1s_3	[tata]
r_2s_1	[tadta]
r_2s_2	[tadda]
r_2s_3	[tata]
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r_3s_2	[ada]
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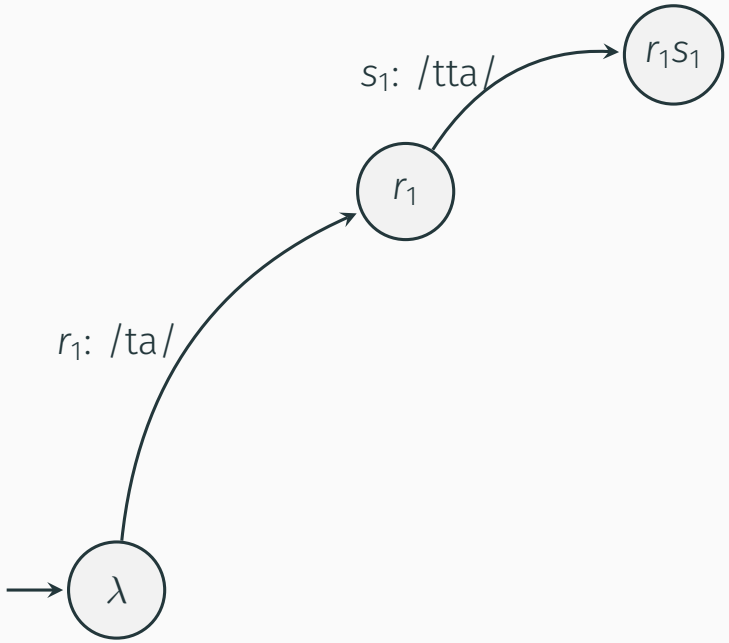

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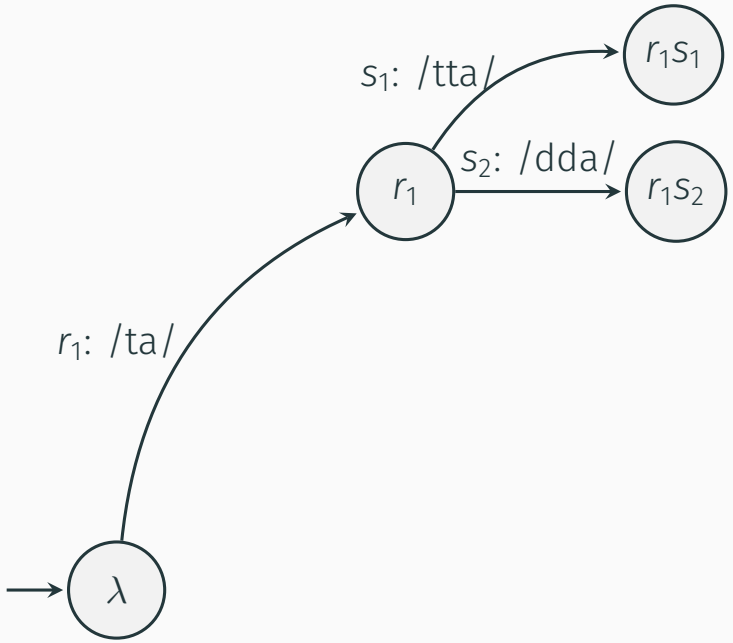

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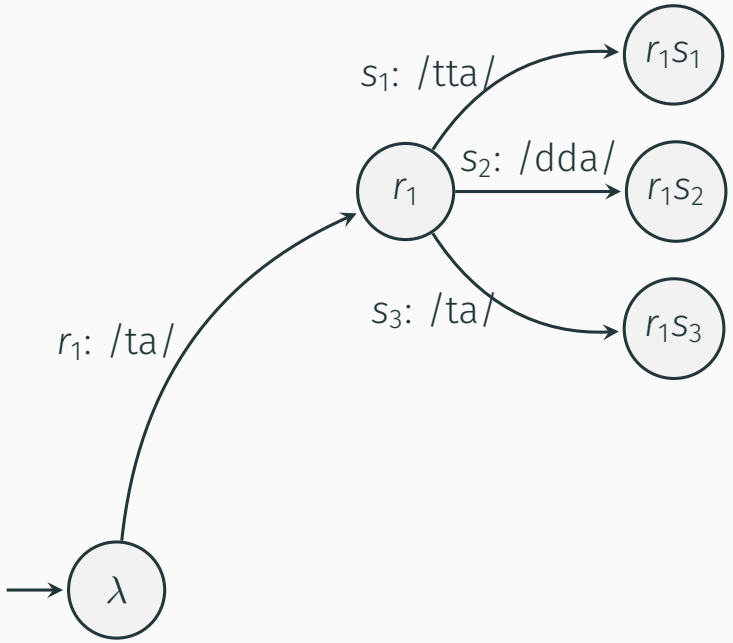

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r_2s_3	[tata]
r_3s_1	[ata]
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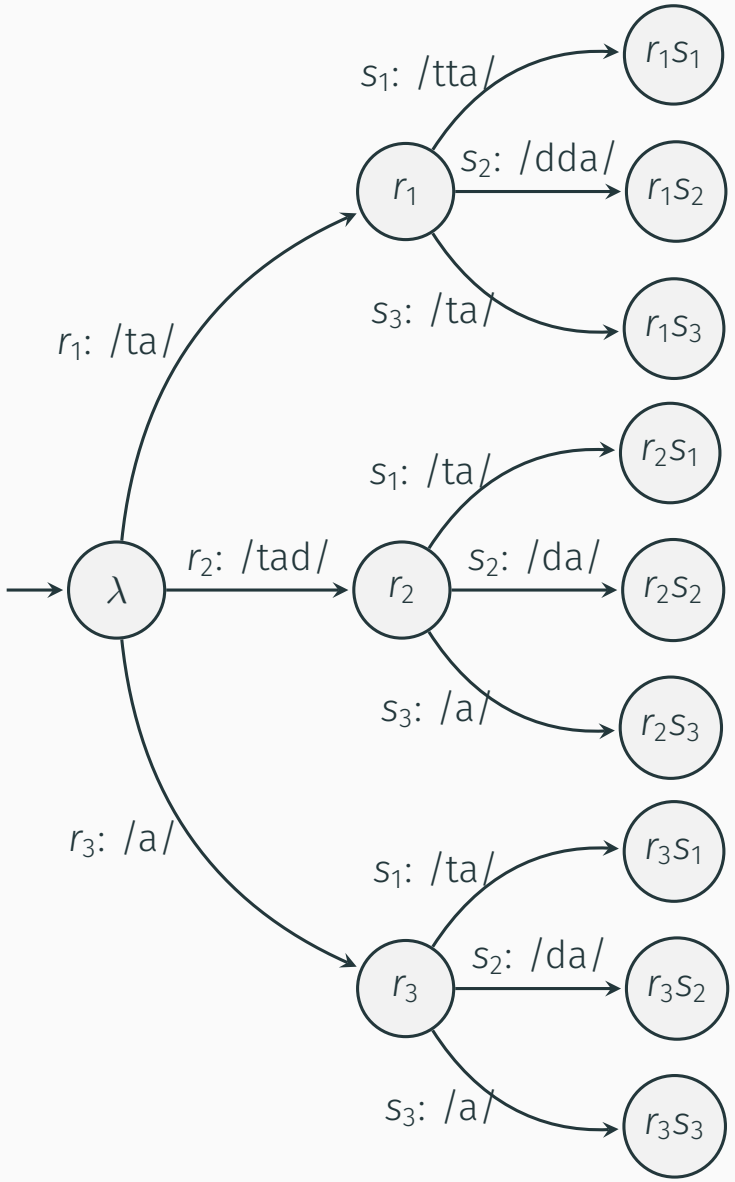

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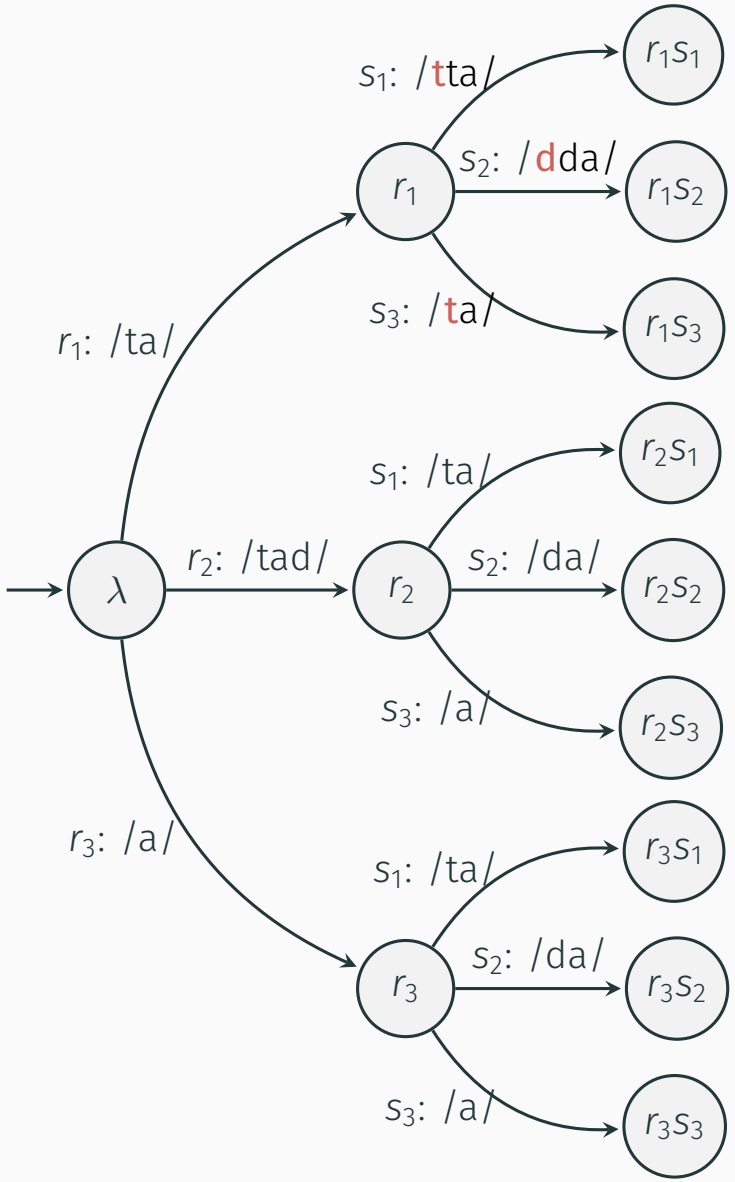
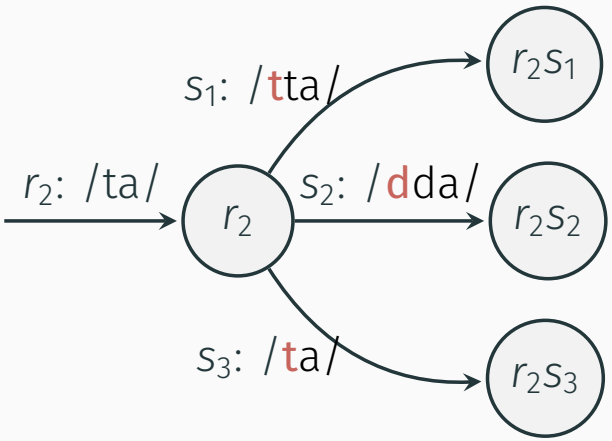
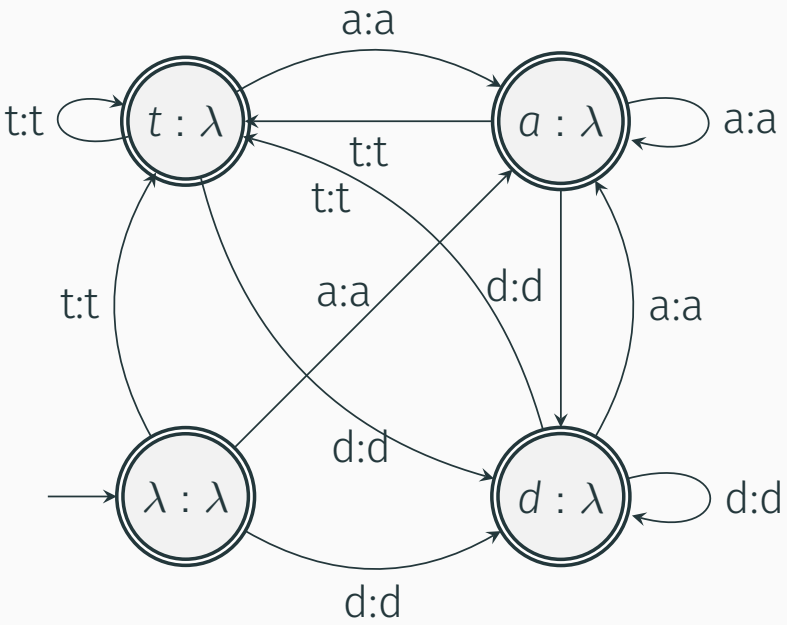
r_3s_2	[ada]
r_3s_3	[aa]



Modifying Transducers

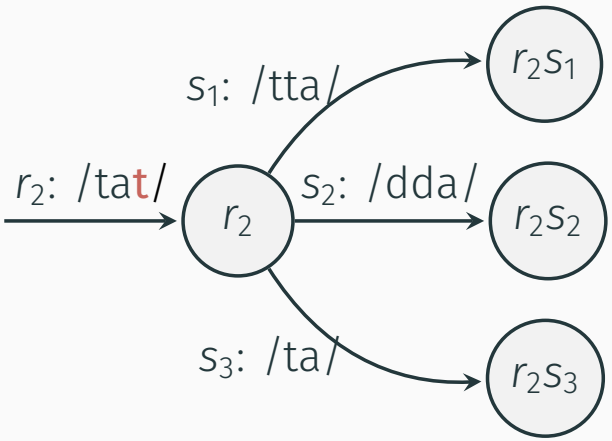
Change SR into UR in the prefix-tree transducer.
Make an opposite change in the phonology transducer.

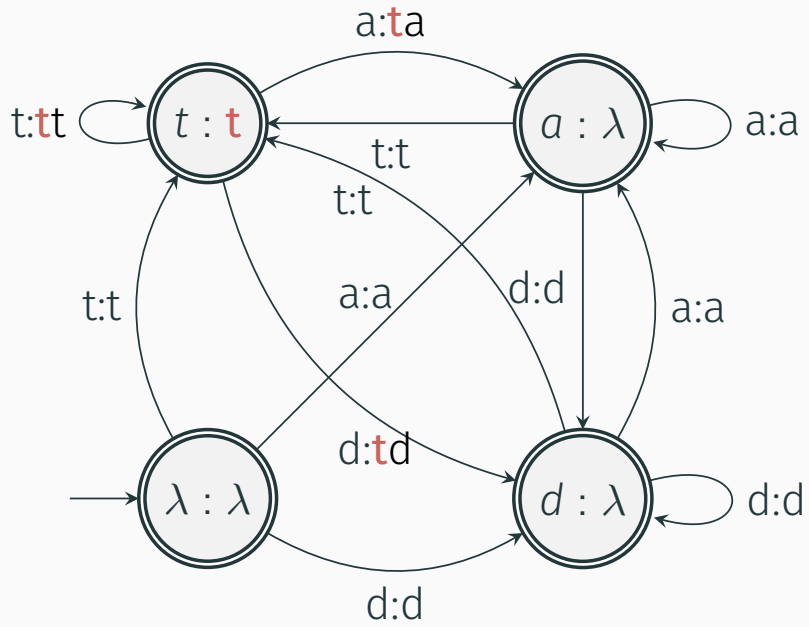




Modifying Transducers

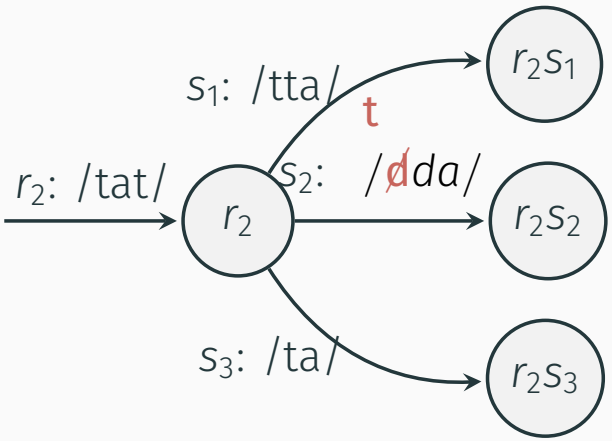
Change SR into UR in the prefix-tree transducer.
Make an opposite change in the phonology transducer.

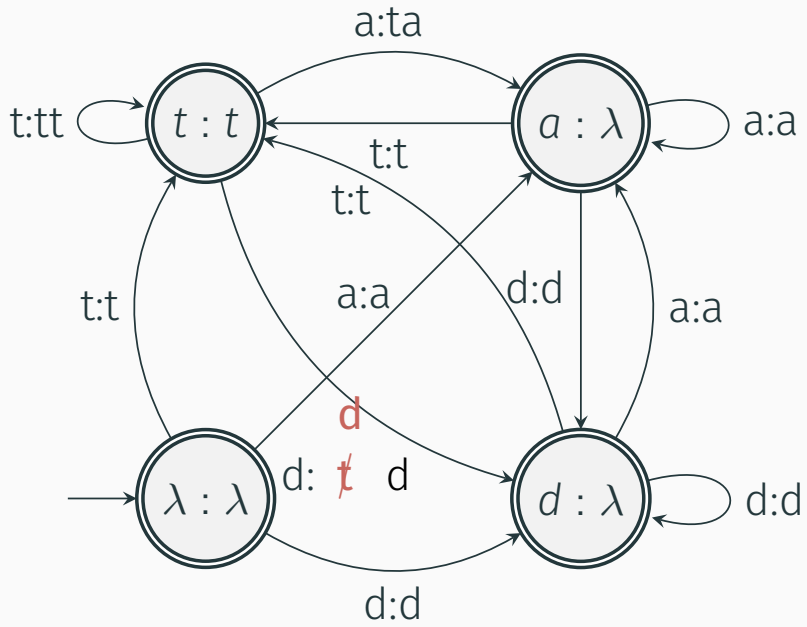




Modifying Transducers

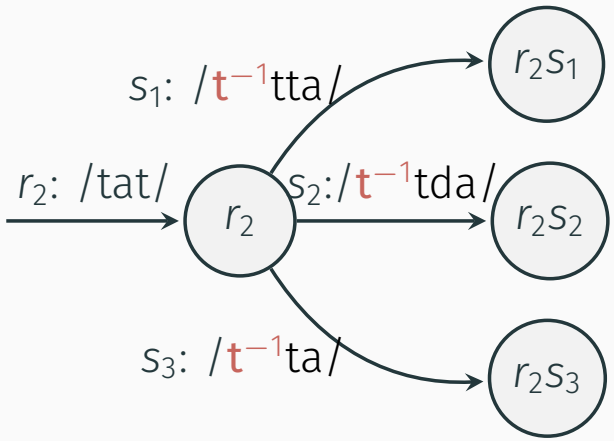
Change SR into UR in the prefix-tree transducer.
Make an opposite change in the phonology transducer.

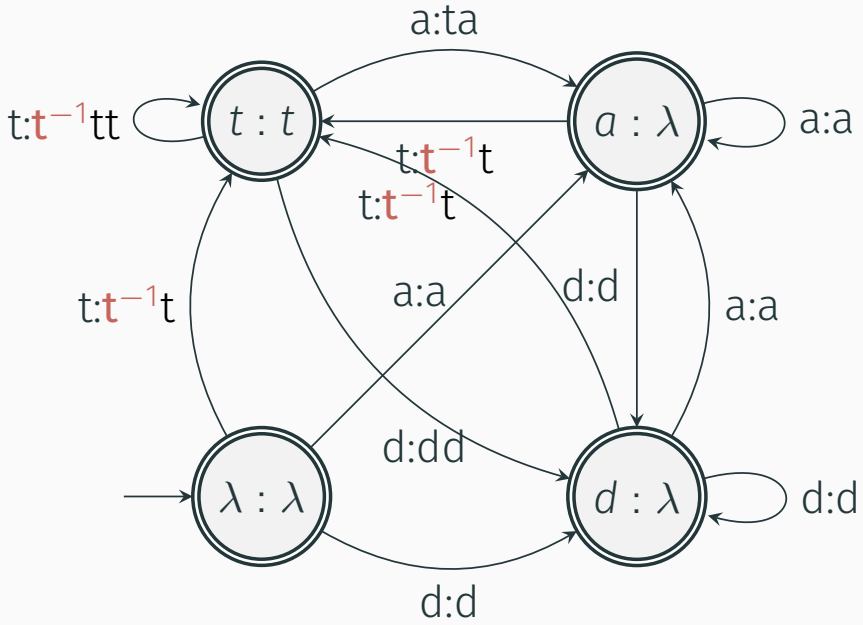




Modifying Transducers

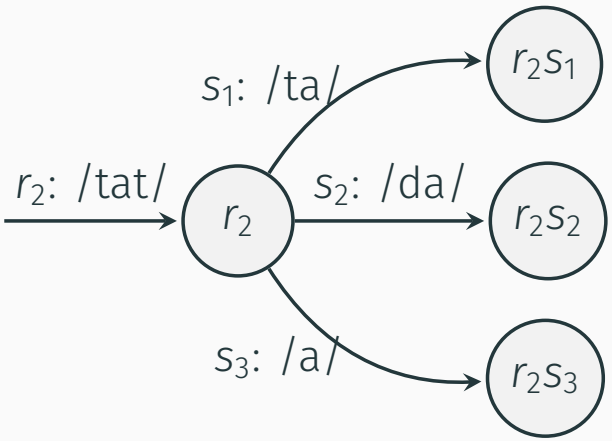
Change SR into UR in the prefix-tree transducer.
Make an opposite change in the phonology transducer.

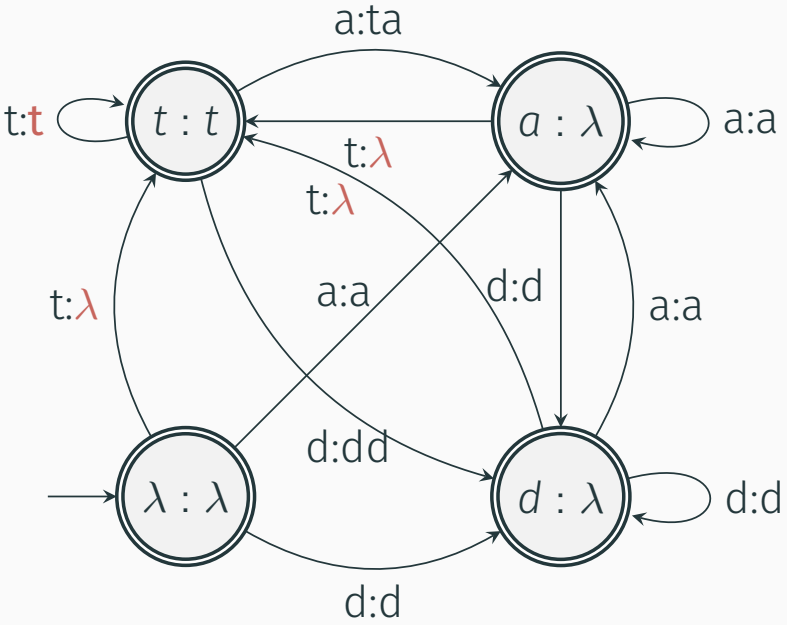




Modifying Transducers

Change SR into UR in the prefix-tree transducer.
Make an opposite change in the phonology transducer.





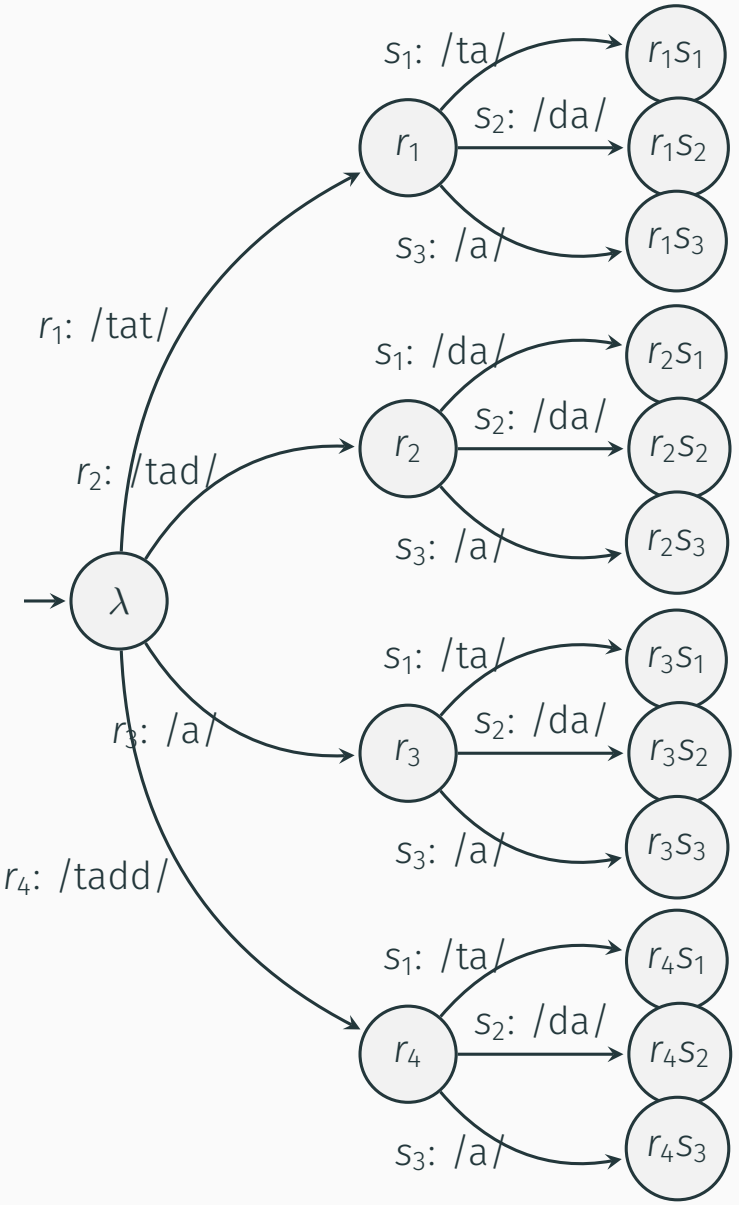
Opacity

- counter-feeding
- counter-bleeding

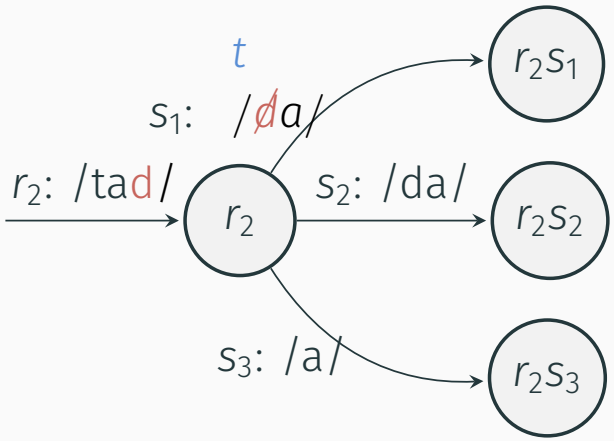
Counter-feeding

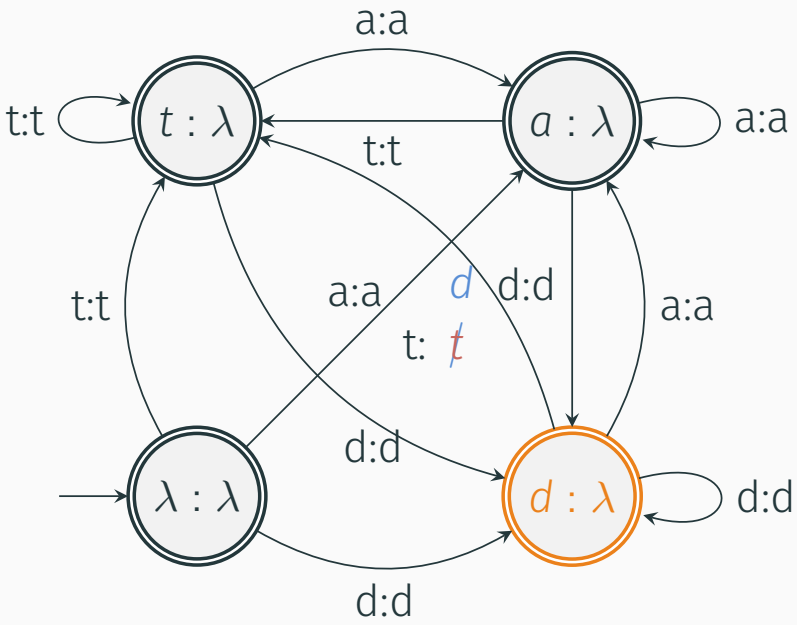
/t/ becomes a voiced [d] after /d/.

m	*s*
r_1s_1	[tatta]
r_1s_2	[tatda]
r_1s_3	[tata]
r_2s_1	[tadda]
r_2s_2	[tadda]
r_2s_3	[tada]
r_3s_1	[ata]
r_3s_2	[ada]
r_3s_3	[aa]
r_4s_1	[taddta]
r_4s_2	[taddda]
r_4s_3	[tadda]

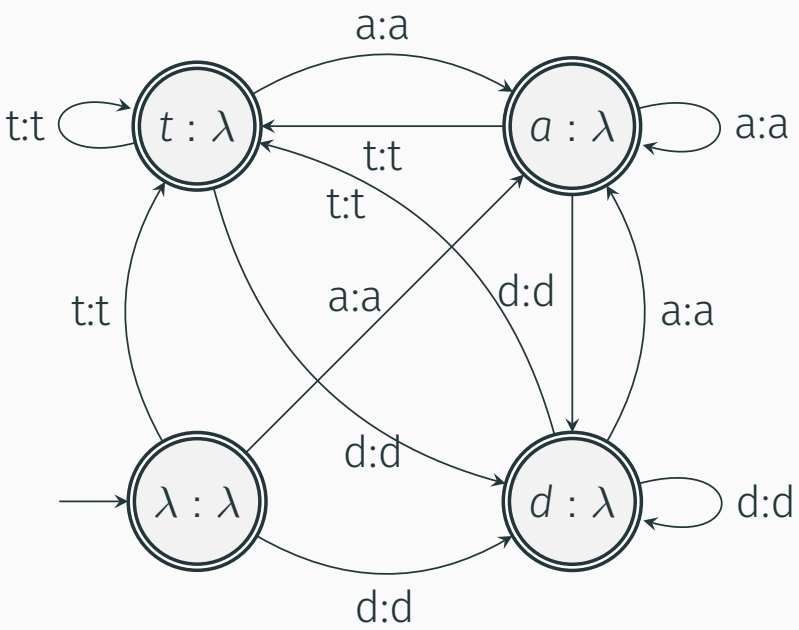


Modified Transducer



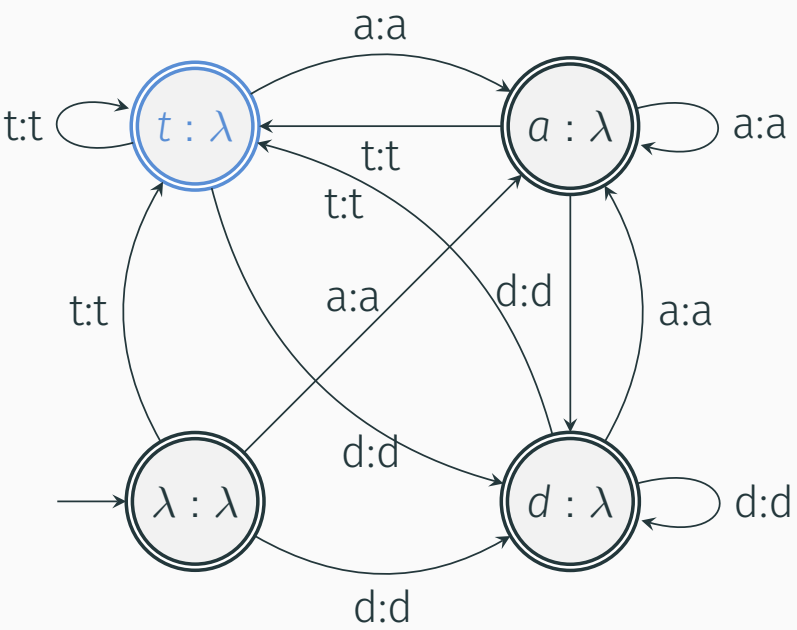


What about the environment?



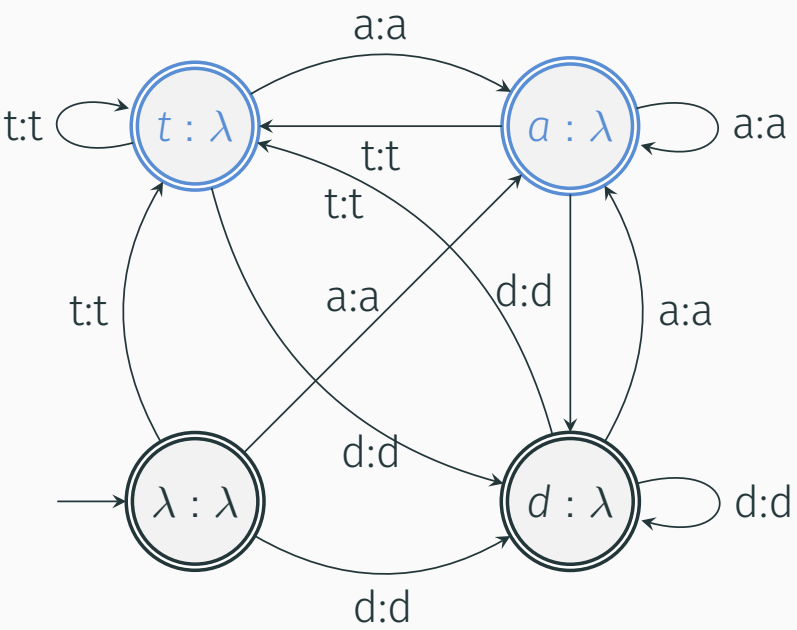
environment	s_1

What about the environment?



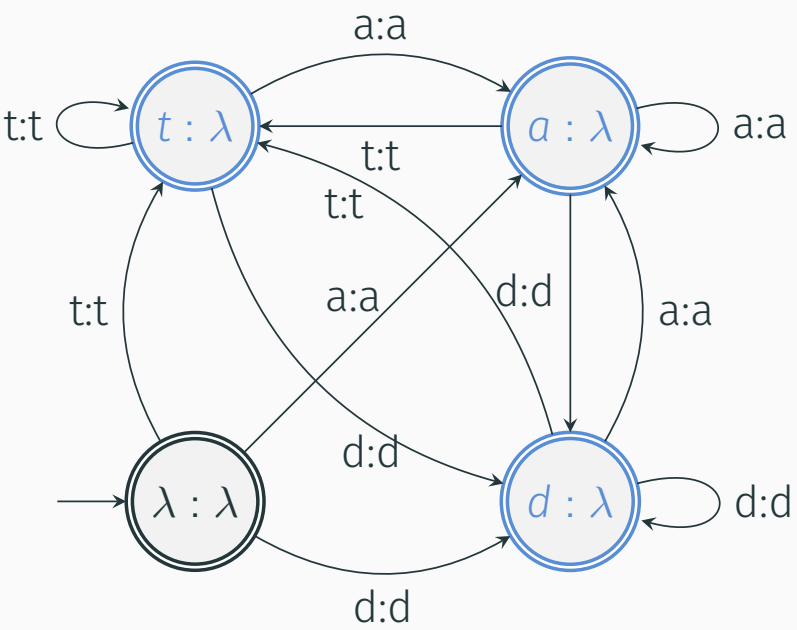
	environment	s_1
$r_1 s_1$	tat	ta

What about the environment?



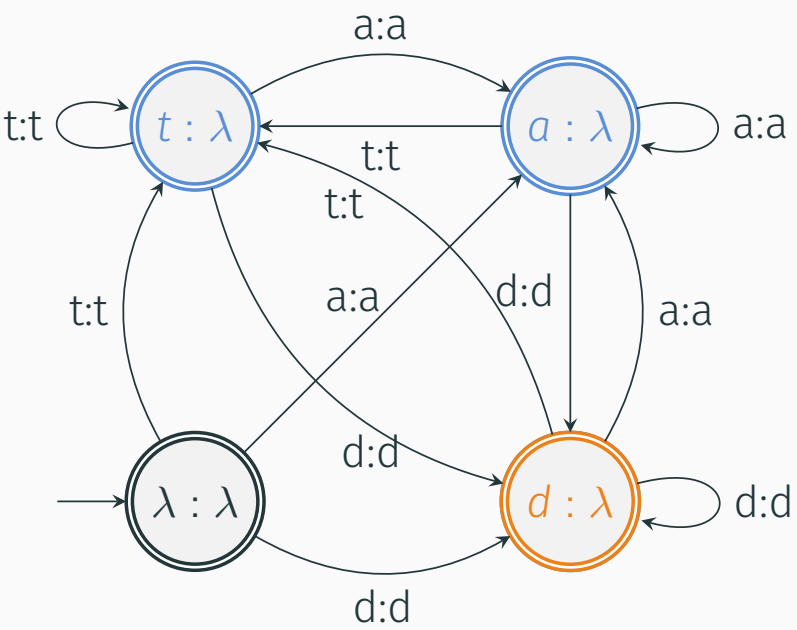
	environment	s_1
$r_1 s_1$	tat	ta
$r_3 s_1$	a	ta

What about the environment?



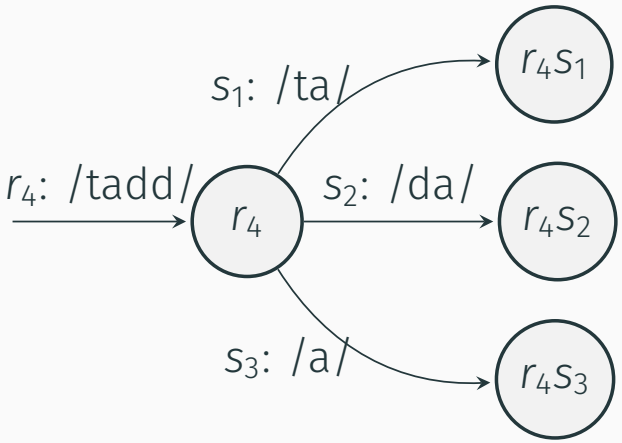
	environment	s_1
$r_1 s_1$	tat	ta
$r_3 s_1$	a	ta
$r_4 s_1$	tadd	ta

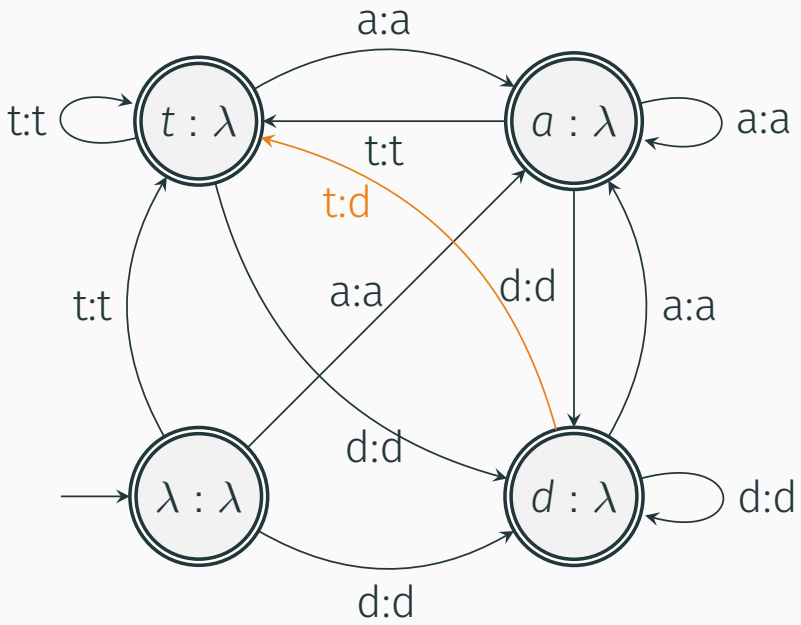
What about the environment?



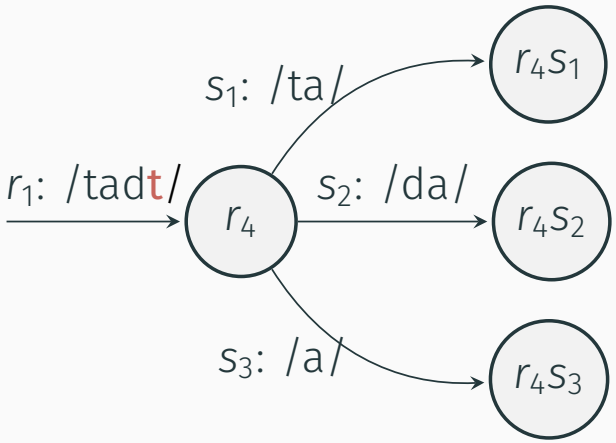
	environment	s_1
$r_1 s_1$	tat	ta
$r_3 s_1$	a	ta
$r_4 s_1$	tadd	ta
$r_2 s_1$	tad	da

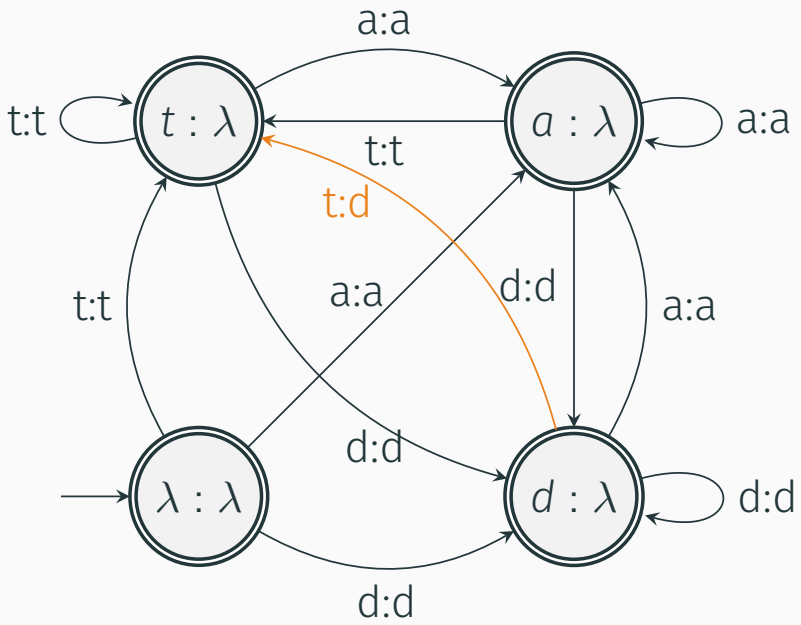
What should we do about the clash of the environment?





What should we do about the clash of the environment?





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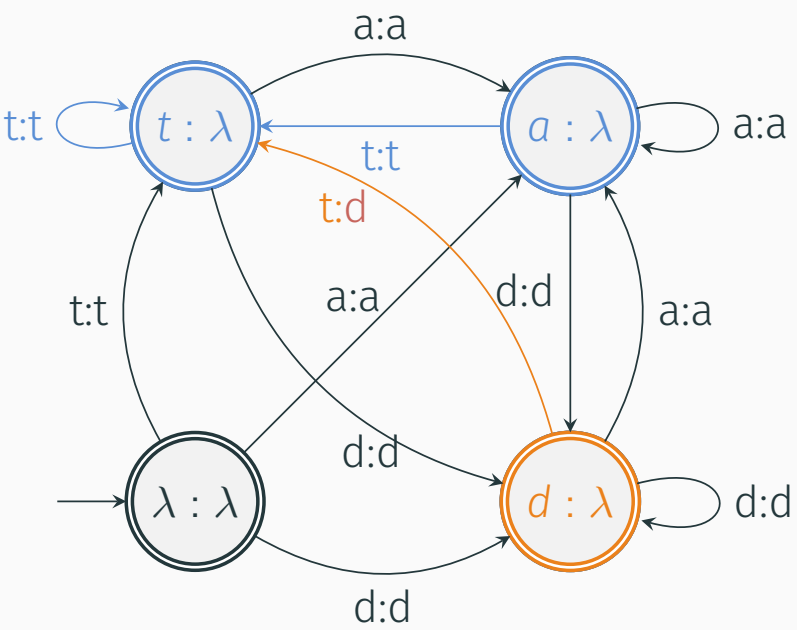

	environment	s_1
$r_1 s_1$	tat	ta
$r_3 s_1$	a	ta
$r_4 s_1$	tadt	ta
$r_2 s_1$	tad	da

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